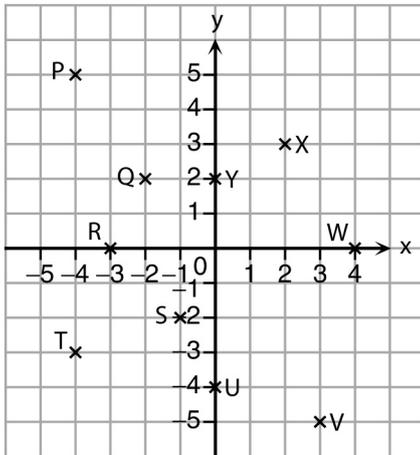


Set 1 Q

Consider the rectangular coordinate plane below.



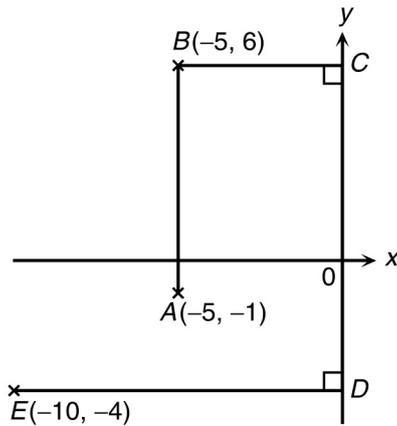
- (a) Write down the points which lie in the
  - (i) 2nd quadrant,
  - (ii) 3rd quadrant.
- (b) Write down the  $x$ -coordinates of  $Q$  and  $U$ .
- (c) Write down the  $y$ -coordinates of  $T$  and  $Y$ .
- (d) Write down the coordinates of  $W$ ,  $P$ ,  $S$  and  $V$ .

- (a) Plot four points  $A(2, 3)$ ,  $B(-4, 0)$ ,  $C(-4, -3)$  and  $D(3, 4)$  on a rectangular coordinate plane.
- (b) Join  $A$  and  $B$ . Write down the coordinates of the point of intersection of  $AB$  and the  $y$ -axis.
- (c) Join  $C$  and  $D$ . Write down the coordinates of the point of intersection of  $CD$  and the  $x$ -axis.

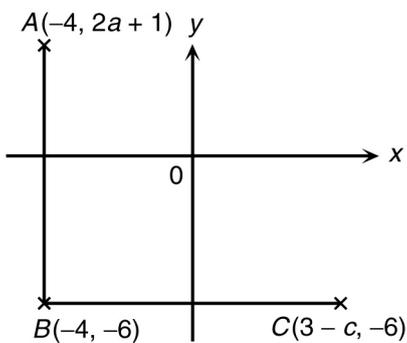
Find the distance between  $A(-3, -2)$  and  $B(-8, -2)$ .

Find the distance between  $P(2, -5)$  and  $Q(2, 4)$ .

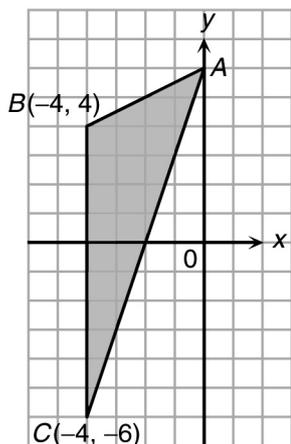
The figure shows five points  $A(-5, -1)$ ,  $B(-5, 6)$ ,  $C$ ,  $D$  and  $E(-10, -4)$ .  $C$  and  $D$  are points on the  $y$ -axis such that  $BC$  and  $DE$  are two horizontal lines. If a man walks from  $A$  via  $B$ ,  $C$  and  $D$  to  $E$ , find the total distance he travels.



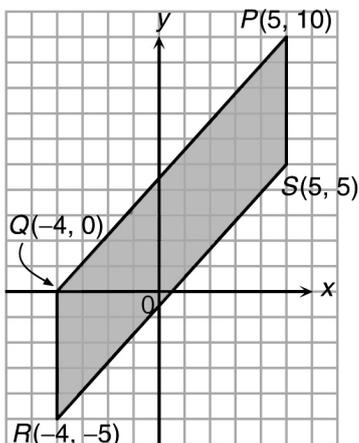
The figure shows three points  $A(-4, 2a + 1)$ ,  $B(-4, -6)$  and  $C(3 - c, -6)$ . Given that  $AB = 9$  units and  $BC = 8$  units, find  $a$  and  $c$ .



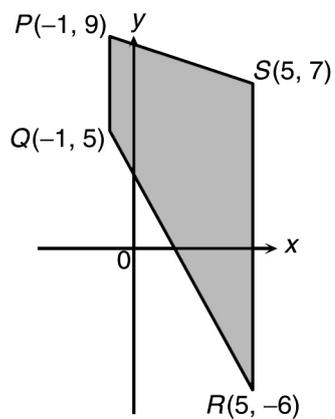
In the figure,  $A$ ,  $B(-4, 4)$  and  $C(-4, -6)$  are the vertices of  $\triangle ABC$ , where  $A$  lies on the  $y$ -axis. Find the area of  $\triangle ABC$ .



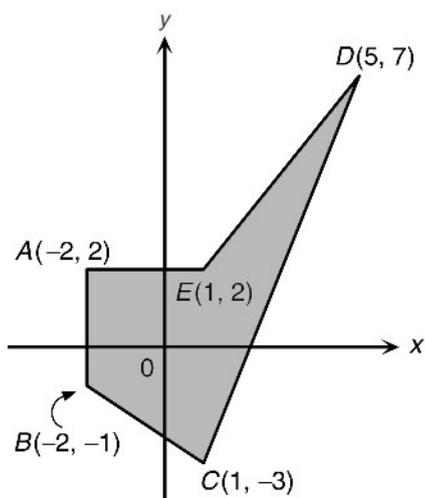
Find the area of parallelogram  $PQRS$  in the figure.



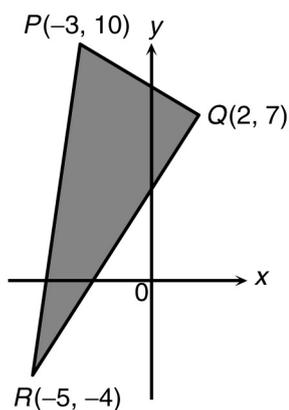
Find the area of trapezium  $PQRS$  in the figure.



Find the area of pentagon  $ABCDE$  in the figure.



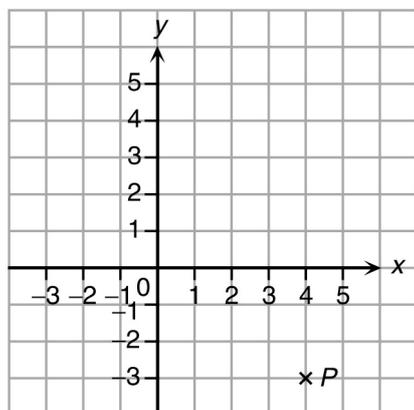
Find the area of  $\triangle PQR$  in the figure.



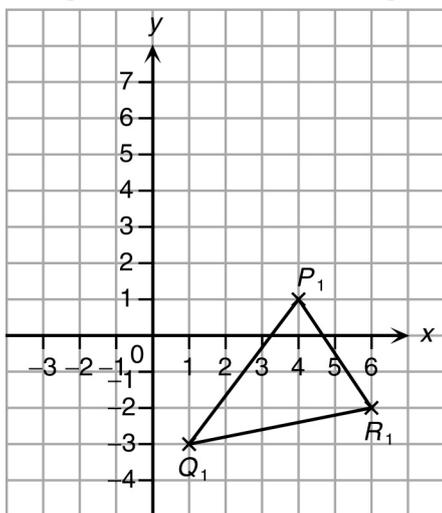
The figure shows a point  $P(4, -3)$ . Then  $P$  is translated upwards by 8 units to  $P_1$ .

(a) Find the coordinates of  $P_1$ .

(b) If  $P_1$  is translated to the left by 7 units and then translated downwards by 3 units to  $P_2$ , find the coordinates of  $P_2$ .



$P$ ,  $Q$  and  $R$  are translated to the right by 4 units and then translated downwards by 6 units to  $P_1(4, 1)$ ,  $Q_1(1, -3)$  and  $R_1(6, -2)$ . Find the coordinates of the vertices of  $\triangle PQR$  and hence draw  $\triangle PQR$  in the figure.



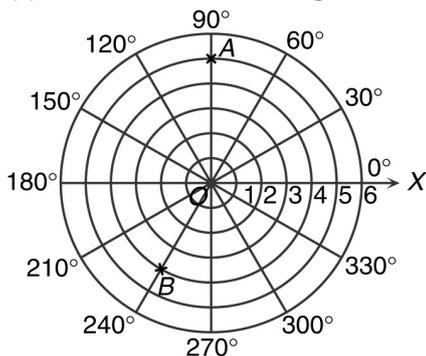
$P(-5, 2)$  is a point on a rectangular coordinate plane. If  $P$  is reflected about the  $y$ -axis to  $Q$  and  $Q$  is reflected about the  $x$ -axis to  $R$ , write down the coordinates of  $Q$  and  $R$ .

If  $P(4, -6)$  is rotated through  $90^\circ$  anti-clockwise about  $O$  to  $Q$ , find the coordinates of  $Q$ .

Consider a point  $P(-2, -5)$  on a rectangular coordinate plane.

- (a) If  $P$  is rotated through  $180^\circ$  anti-clockwise about  $O$  to  $Q$ , find the coordinates of  $Q$ .
- (b) If a point  $R$  is rotated through  $270^\circ$  anti-clockwise about  $O$  to  $P$ , find the coordinates of  $R$ .

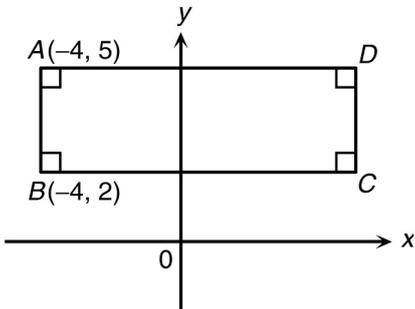
- (a) Write down the polar coordinates of  $A$  and  $B$  on the polar coordinate plane.
- (b) Plot  $P(3, 150^\circ)$  and  $Q(2, 270^\circ)$  on the polar coordinate plane.
- (c) Find  $\angle POB$  and  $AQ$ .



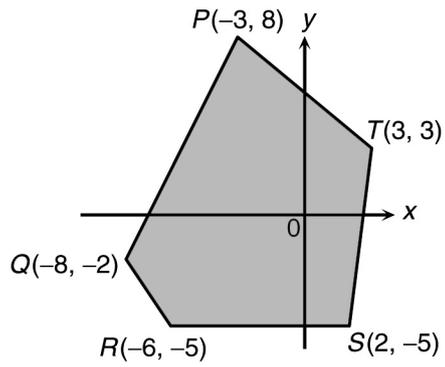
- (a) Plot four points  $A(-4, 1)$ ,  $B(-1, -2)$ ,  $C(6, 1)$  and  $D(3, 4)$  on a rectangular coordinate plane.
- (b) Join  $AB$ ,  $BC$ ,  $CD$  and  $DA$ .
- (c) Find the coordinates of the point of intersection of the diagonals of  $ABCD$ .
- (d) Which type of quadrilateral is  $ABCD$ ?

In the figure,  $ABCD$  is a rectangle with  $AD = 3AB$ .

- (a) Find the length of  $AB$ .
- (b) Hence, find the length of  $AD$ .
- (c) Find the coordinates of  $C$  and  $D$ .



Find the area of pentagon  $PQRST$  in the figure.

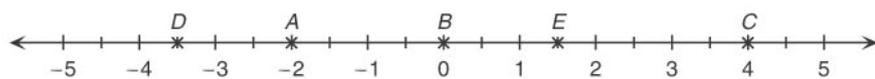


A point  $P(a, b)$  is translated to the left by 5 units, and then reflected about the  $x$ -axis, and then rotated through  $90^\circ$  clockwise about  $O$  to  $Q(-2, 8)$ . Find the values of  $a$  and  $b$ .

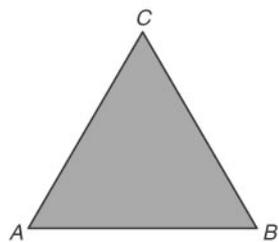
# Ch 10. Introduction to Coordinates

## Set 2 Q

Find the directed numbers represented by the letters on the number line below.

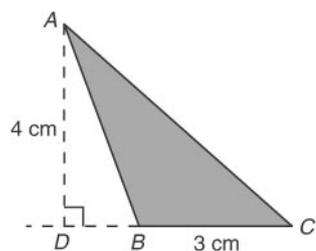


Rotate equilateral triangle  $ABC$  through  $180^\circ$  anti-clockwise about  $A$ .

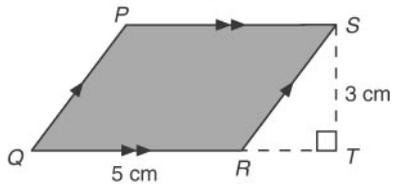


Draw a vertical number line from  $-4$  to  $4$  and label  $-\frac{1}{2}$ ,  $+1.5$ ,  $0$ ,  $3$ ,  $-2.5$  on it.

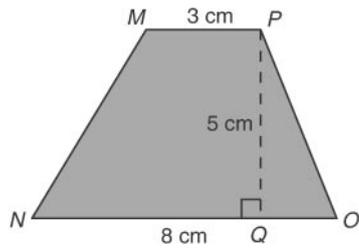
Find the area of  $\triangle ABC$ .



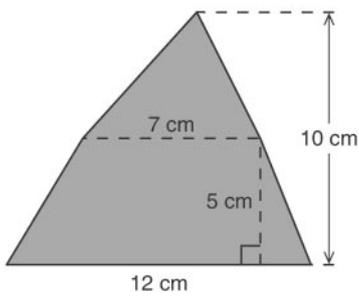
Find the area of parallelogram  $PQRS$ .



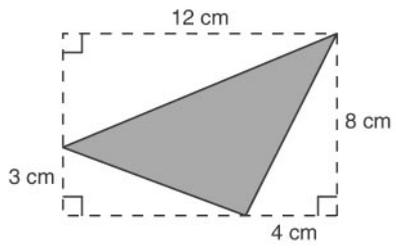
Find the area of trapezium  $MNOP$ .



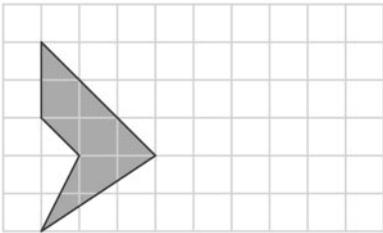
Find the area of the figure.



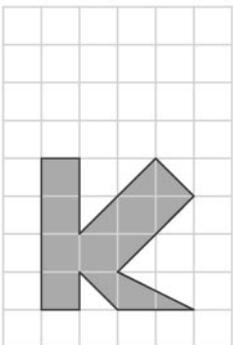
Find the area of the figure.



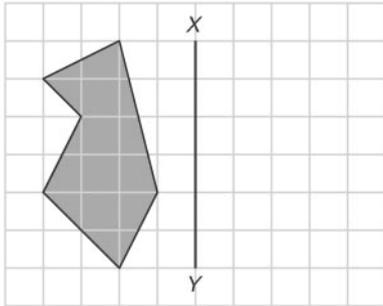
Translate the figure to the right by 3 units.



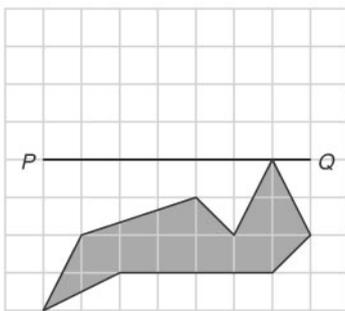
Translate the figure upwards by 2 units.



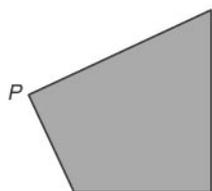
Reflect the figure about  $XY$ .



Reflect the figure about  $PQ$ .



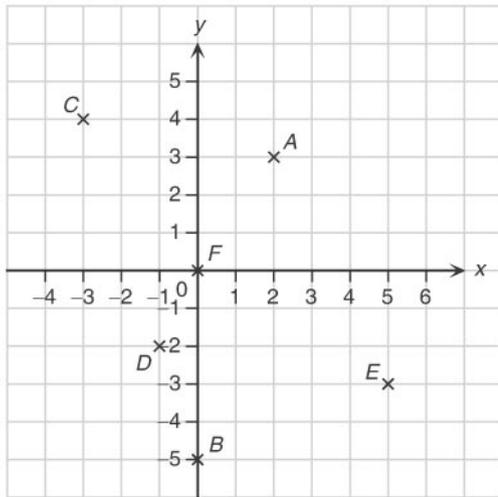
Rotate the following figure through  $90^\circ$  anti-clockwise about  $P$ .



## Ch 10. Introduction to Coordinates

### Set 3 Q

In the figure, write down the coordinates of points  $A$  to  $F$ .



Which quadrants do the following points lie in?

- (a)  $P(6, 7)$
- (b)  $Q(-2, -2)$
- (c)  $R(2.5, -3.5)$
- (d)  $S\left(-\frac{3}{8}, 1\frac{7}{10}\right)$

Plot four points  $A(-3, 4)$ ,  $B(0, 2)$ ,  $C(2, 0)$  and  $D(5, -1)$  on a rectangular coordinate plane. Write down the  $x$ -coordinates of these points.

Plot four points  $E(1, 1)$ ,  $F(-3, 0)$ ,  $G(0, -3)$  and  $H(-2, -2)$  on a rectangular coordinate plane. Write down the  $y$ -coordinates of these points.

If  $M(a, b)$  and  $N(c, d)$  lie on the  $x$ -axis and the  $y$ -axis respectively, find  $b$  and  $c$ .

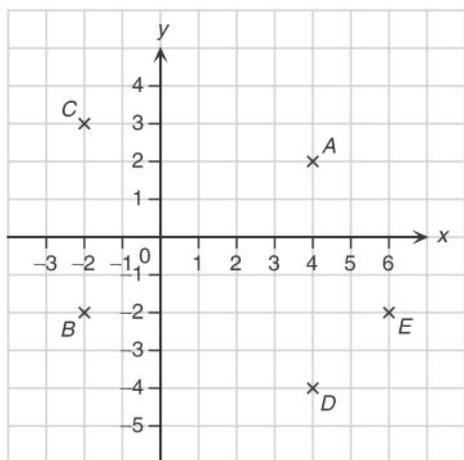
- (a) Plot the following points on a rectangular coordinate plane:  $A(-2, -2)$ ,  $B(-2, 2)$ ,  $C(1, 0)$ ,  $D(4, 2)$  and  $E(4, -2)$
- (b) Join  $AB$ ,  $BC$ ,  $CD$  and  $DE$ . Which letter is formed?

- (a) Plot  $P(-1, 1)$ ,  $Q(3, -4)$  and  $R(3, 1)$  on a rectangular coordinate plane.
- (b) What kind of triangle is  $\triangle PQR$ ?

- (a) Plot the following points on a rectangular coordinate plane:  $A(-1, -6)$ ,  $B(5, -6)$ ,  $C(5, -5)$ ,  $D(0, -5)$ ,  $E(0, -2)$ ,  $F(5, -2)$ ,  $G(5, -1)$  and  $H(-1, -1)$
- (b) What kind of polygon is  $ABCDEFGH$ ?

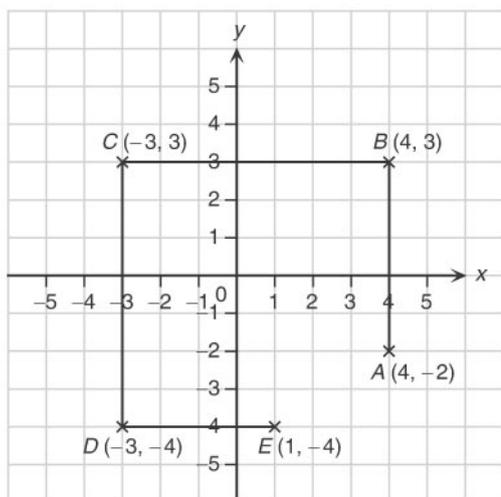
- (a) Plot  $A(-2, -4)$  and  $B(3, 1)$  on a rectangular coordinate plane.
- (b) Draw a line  $L$  passing through  $A$  and  $B$ . If  $L$  intersects the  $x$ -axis at  $P$  and the  $y$ -axis at  $Q$ , find the coordinates of  $P$  and  $Q$ .

The figure shows points  $A$  to  $E$  on a rectangular coordinate plane.



- (a) Join  $AB$ ,  $AD$ ,  $BC$ ,  $BE$  and  $DE$ .
- (b) Which line in (a) is parallel to the  $x$ -axis?
- (c) Which line(s) in (a) is/are parallel to the  $y$ -axis?

Find the lengths of line segments  $AB$ ,  $BC$ ,  $CD$  and  $DE$  in the figure.



Find the distance between  $A(2, 7)$  and  $B(2, 0)$ .

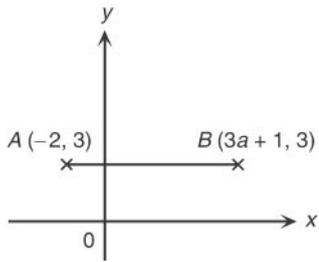
Find the distance between  $C(6, -3)$  and  $D(-4, -3)$ .

Find the distance between  $E(-1.2, 4.5)$  and  $F(-1.2, -3.4)$ .

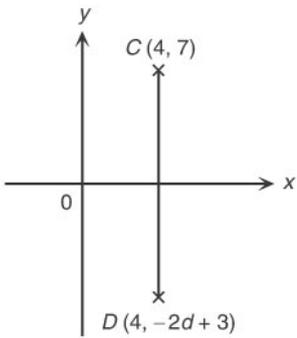
Find the distance between  $G\left(5\frac{1}{2}, -\frac{2}{3}\right)$  and  $H\left(5\frac{1}{2}, -3\frac{1}{6}\right)$ .

Given three points  $A(1, 1)$ ,  $B(3, 1)$  and  $C(3, -1)$ , find  $AB$  and  $BC$ .

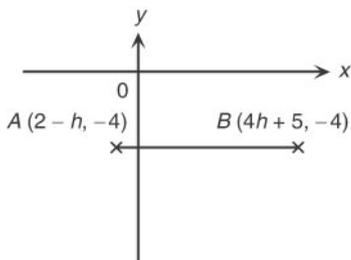
In the figure,  $A(-2, 3)$  is on the left of  $B(3a + 1, 3)$ . If  $AB = 9$  units, find  $a$ .



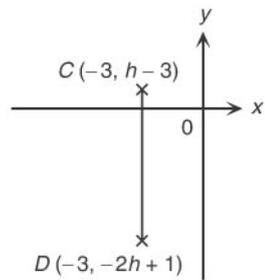
In the figure,  $C(4, 7)$  is above  $D(4, -2d + 3)$ . If  $CD = 14$  units, find  $d$ .



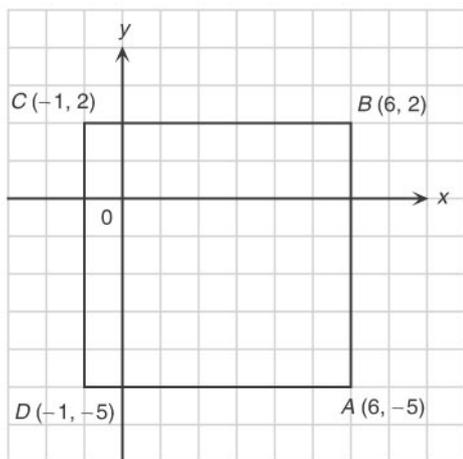
In the figure,  $A(2 - h, -4)$  is on the left of  $B(4h + 5, -4)$ . If  $AB = 7\frac{1}{4}$  units, find  $h$ .



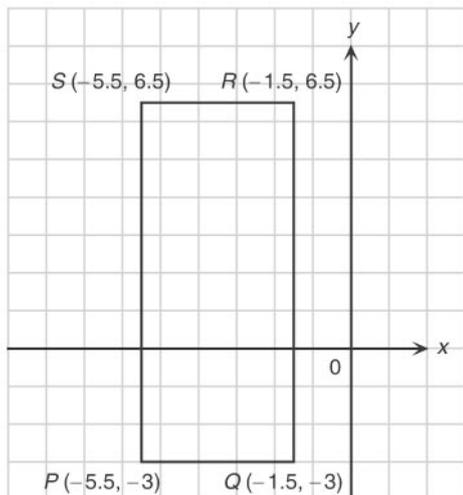
In the figure,  $C(-3, h - 3)$  is above  $D(-3, -2h + 1)$ . If  $CD = 8$  units, find  $h$ .



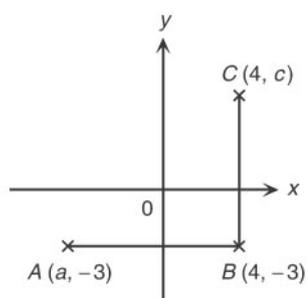
There are four points  $A(6, -5)$ ,  $B(6, 2)$ ,  $C(-1, 2)$  and  $D(-1, -5)$  in the figure. Find the perimeter of quadrilateral  $ABCD$ .



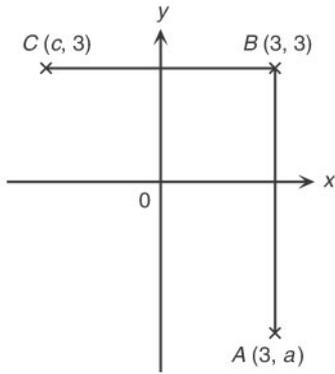
There are four points  $P(-5.5, -3)$ ,  $Q(-1.5, -3)$ ,  $R(-1.5, 6.5)$  and  $S(-5.5, 6.5)$  in the figure. Find the perimeter of quadrilateral  $PQRS$ .



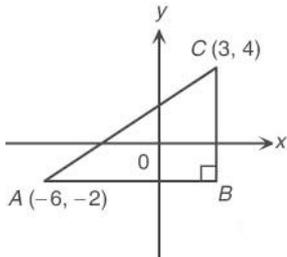
There are three points  $A(a, -3)$ ,  $B(4, -3)$  and  $C(4, c)$  in the figure. If  $AB = 9$  units and  $BC = 8$  units, find  $a$  and  $c$ .



There are three points  $A(3, a)$ ,  $B(3, 3)$  and  $C(c, 3)$  in the figure. If  $AB = 7$  units and  $BC = 6$  units, find  $a$  and  $c$ .

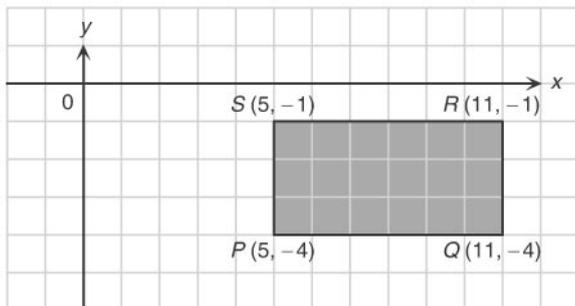


In the figure,  $AB$  is parallel to the  $x$ -axis and  $BC$  is parallel to the  $y$ -axis.

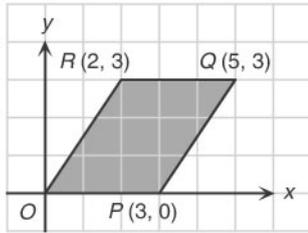


- (a) Find the coordinates of  $B$ .
- (b) Find  $AB$  and  $BC$ .

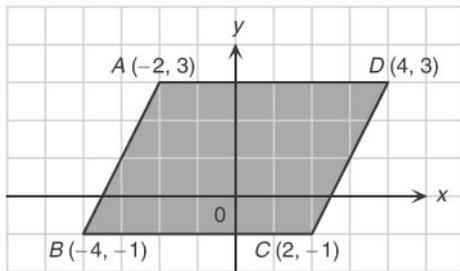
Find the area of rectangle  $PQRS$  in the figure.



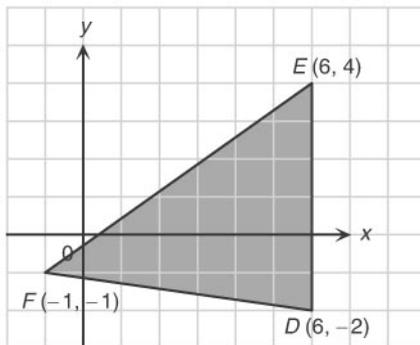
Find the area of parallelogram  $OPQR$  in the figure.



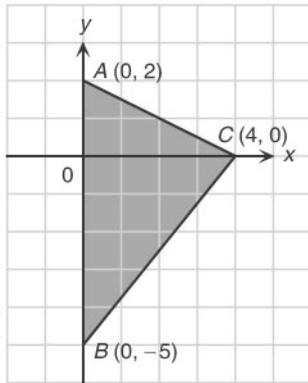
Find the area of parallelogram  $ABCD$  in the figure.



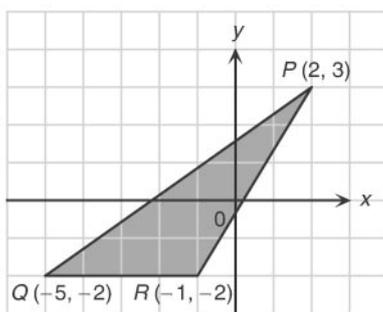
Find the area of  $\triangle DEF$  in the figure.



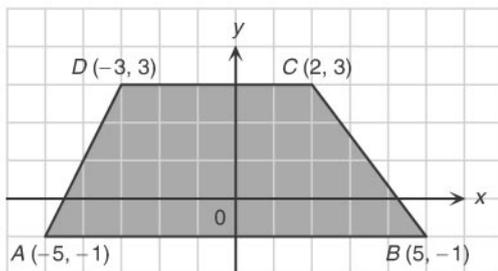
Find the area of  $\triangle ABC$  in the figure.



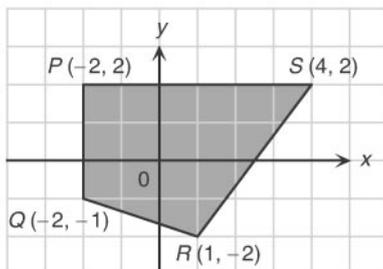
Find the area of  $\triangle PQR$  in the figure.



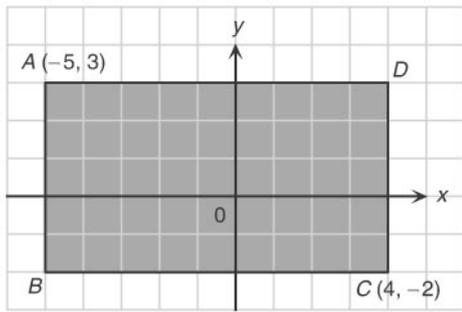
Find the area of trapezium ABCD in the figure.



Find the area of quadrilateral PQRS in the figure.



In the figure,  $A(-5, 3)$  and  $C(4, -2)$  are two vertices of rectangle  $ABCD$ . Given that  $AD$  is parallel to the  $x$ -axis, find



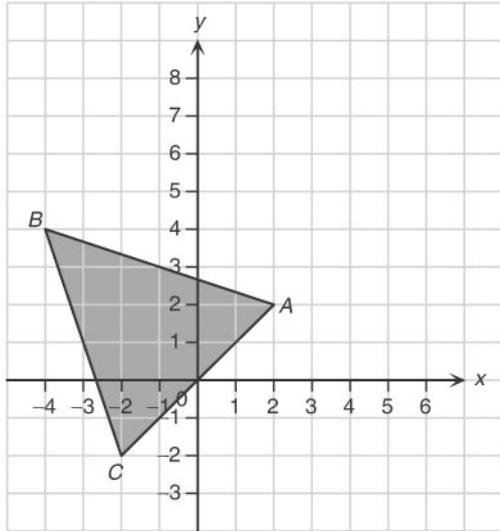
- (a) the coordinates of  $B$  and  $D$ ,
- (b) the area of rectangle  $ABCD$ .

- (a) Draw a trapezium  $ABCD$  with vertices  $A(4, 2)$ ,  $B(0, 2)$ ,  $C(-2, -2)$  and  $D(5, -2)$  on a rectangle coordinate plane.
- (b) Find the area of trapezium  $ABCD$ .

Plot the point  $A(-4, -5)$  on a rectangular coordinate plane. Then plot  $A_1$ ,  $A_2$  and  $A_3$  according to the instructions below and write down their coordinates.

- (a)  $A$  is translated to the right by 6 units to  $A_1$ .
- (b)  $A$  is translated upwards by 10 units to  $A_2$ .
- (c)  $A$  is translated to the right by 4 units and then translated upwards by 7 units to  $A_3$ .

The figure shows  $\triangle ABC$ . If  $\triangle ABC$  is translated upwards by 4 units to  $\triangle A_1B_1C_1$ ,

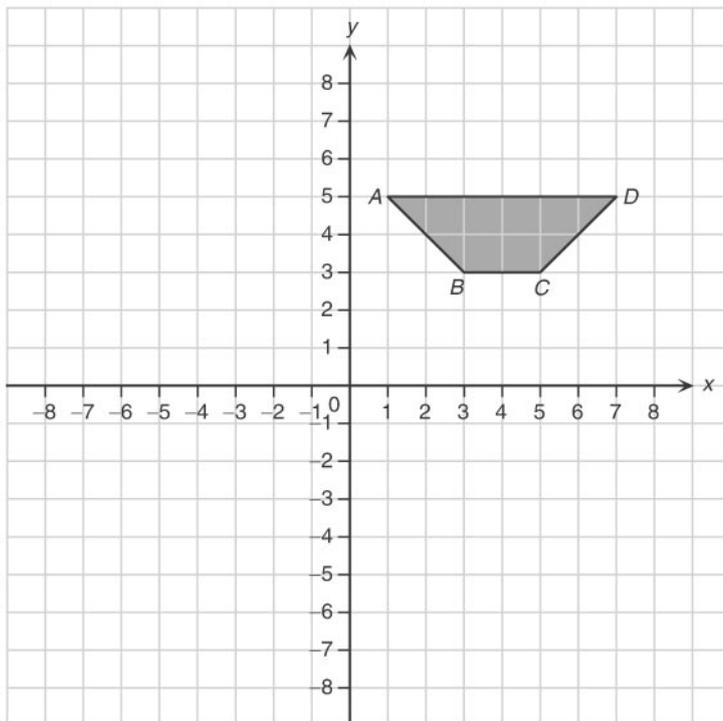


- (a) draw  $\triangle A_1B_1C_1$  in the figure,
- (b) write down the coordinates of the vertices of  $\triangle A_1B_1C_1$ .

- (a) Plot  $A(-2, 3)$ ,  $B(-4, -1)$  and  $C(2, -1)$  on a rectangular coordinate plane.
- (b) If  $A$ ,  $B$  and  $C$  are translated downwards by 2 units to  $A_1$ ,  $B_1$  and  $C_1$  respectively, plot  $A_1$ ,  $B_1$  and  $C_1$  in the figure and write down their coordinates.
- (c) If  $A$ ,  $B$  and  $C$  are translated to the left by 3 units to  $A_2$ ,  $B_2$  and  $C_2$  respectively, plot  $A_2$ ,  $B_2$  and  $C_2$  in the figure and write down their coordinates.

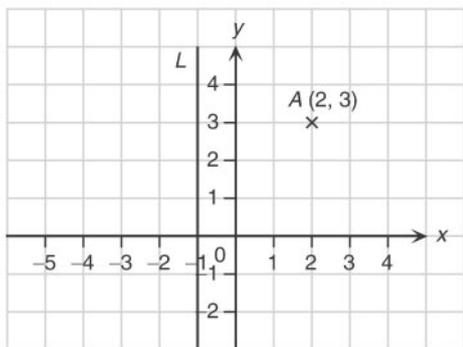
- (a) Plot  $X(2, 4)$  and  $Y(-4, -3)$  on a rectangular coordinate plane.
- (b) If  $X$  and  $Y$  are reflected about the  $x$ -axis to  $X_1$  and  $Y_1$  respectively, plot  $X_1$  and  $Y_1$  in the figure and write down their coordinates.
- (c) If  $X$  and  $Y$  are reflected about the  $y$ -axis to  $X_2$  and  $Y_2$  respectively, plot  $X_2$  and  $Y_2$  in the figure and write down their coordinates.

The figure shows a trapezium  $ABCD$ .



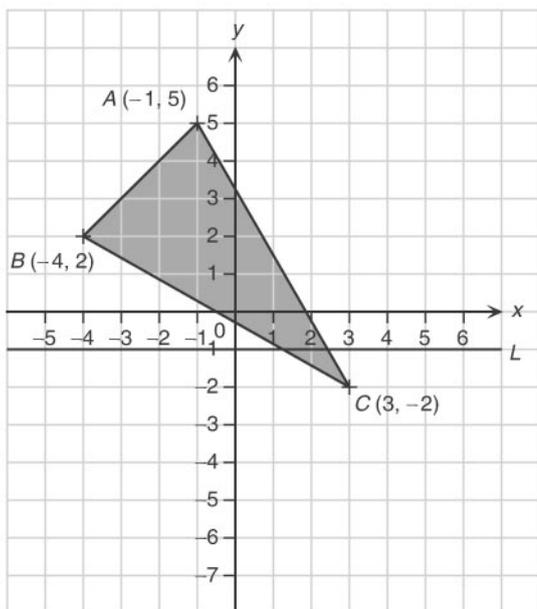
- (a) If trapezium  $ABCD$  is reflected about the  $x$ -axis to trapezium  $A_1B_1C_1D_1$ , draw trapezium  $A_1B_1C_1D_1$  in the figure and write down the coordinates of the vertices of trapezium  $A_1B_1C_1D_1$ .
- (b) If trapezium  $ABCD$  is reflected about the  $y$ -axis to trapezium  $A_2B_2C_2D_2$ , draw trapezium  $A_2B_2C_2D_2$  in the figure and write down the coordinates of the vertices of trapezium  $A_2B_2C_2D_2$ .

The figure shows a point  $A(2, 3)$  on a rectangular coordinate plane.  $L$  is a line parallel to the  $y$ -axis and it passes through  $(-1, 0)$ .



- (a) If  $A$  is reflected about  $L$  to  $A'$ , plot  $A'$  in the figure.
- (b) Write down the coordinates of  $A'$  obtained (a).

The figure shows  $\triangle ABC$ .  $L$  is a line parallel to the  $x$ -axis and it passes through  $(0, -1)$ . If  $\triangle ABC$  is reflected about  $L$  to  $\triangle A_1B_1C_1$ ,

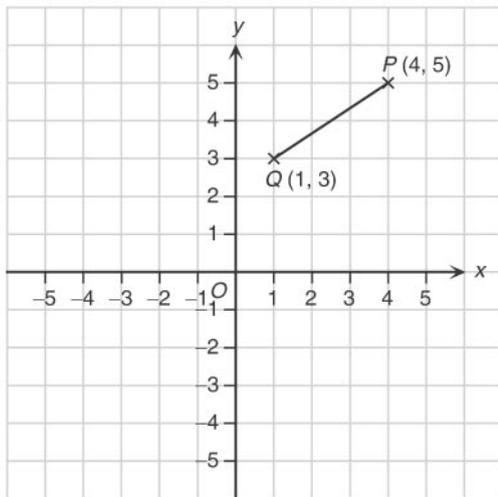


- (a) draw  $\triangle A_1B_1C_1$  in the figure,
- (b) write down the coordinates of the vertices of  $\triangle A_1B_1C_1$ .

Plot  $A(2, 4)$  on a rectangular coordinate plane. Then plot  $A_1$ ,  $A_2$  and  $A_3$  according to the instructions below, and write down their coordinates.

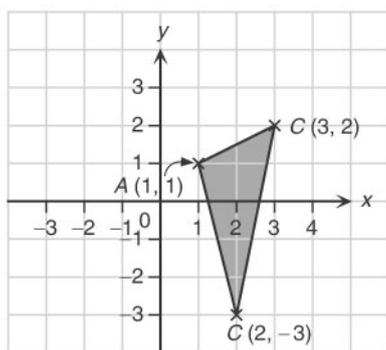
- (a)  $A$  is rotated through  $90^\circ$  anti-clockwise about the origin to  $A_1$ .
- (b)  $A$  is rotated through  $180^\circ$  anti-clockwise about the origin to  $A_2$ .
- (c)  $A$  is rotated through  $270^\circ$  anti-clockwise about the origin to  $A_3$ .

The figure shows a line segment  $PQ$ .



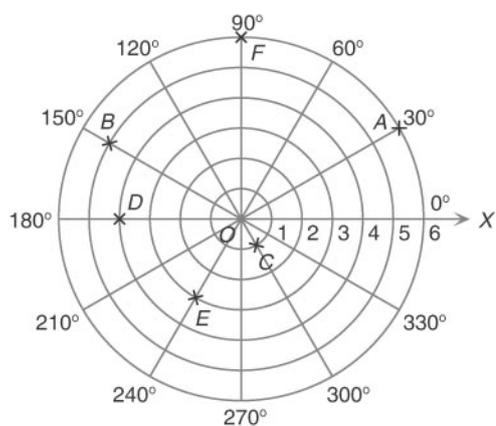
- (a) If  $PQ$  is rotated through  $90^\circ$  anti-clockwise about  $O$  to  $P_1Q_1$ , draw the line segment  $P_1Q_1$  in the figure and write down the coordinates of  $P_1$  and  $Q_1$ .
- (b) If  $PQ$  is rotated through  $180^\circ$  anti-clockwise about  $O$  to  $P_2Q_2$ , draw the line segment  $P_2Q_2$  in the figure and write down the coordinates of  $P_2$  and  $Q_2$ .
- (c) If  $PQ$  is rotated through  $270^\circ$  anti-clockwise about  $O$  to  $P_3Q_3$ , draw the line segment  $P_3Q_3$  in the figure and write down the coordinates of  $P_3$  and  $Q_3$ .

The figure shows  $\triangle ABC$ . If  $\triangle ABC$  is rotated through  $90^\circ$  anti-clockwise about  $O$  to  $\triangle A'B'C'$ ,



- (a) draw  $\triangle A'B'C'$  in the figure,
- (b) write down the coordinates of the vertices of  $\triangle A'B'C'$ .

Write down the polar coordinates of points  $A$  to  $F$  on the polar coordinate plane below.



- (a) Plot  $A(4, 180^\circ)$ ,  $B(4, 240^\circ)$ ,  $C(4, 0^\circ)$  and  $D(4, 60^\circ)$  on a polar coordinate plane.
- (b) Join  $AB$ ,  $BC$ ,  $CD$  and  $DA$ . What kind of quadrilateral is  $ABCD$ ?

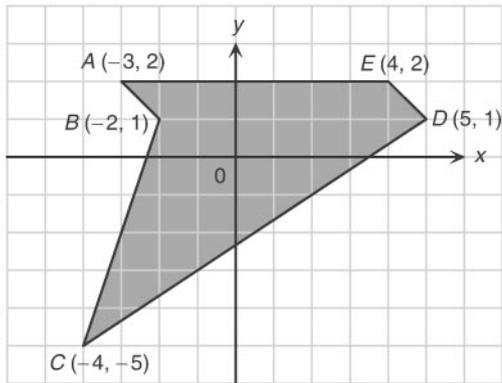
- (a) Plot  $P(1, 90^\circ)$ ,  $Q(2, 210^\circ)$  and  $R(5, 210^\circ)$  on a polar coordinate plane.
- (b) (i) Find  $\angle POQ$ .
- (ii) Find  $QR$ .

## Ch 10. Introduction to Coordinates

### Set 4 Q

If a line  $L$  passes through  $P(3, -5)$  and is parallel to the  $x$ -axis, find the coordinates of the point that  $L$  intersects with the  $y$ -axis.

Find the area of pentagon  $ABCDE$  in the figure.



- (a) Draw  $\triangle PQR$  with vertices  $P(-5, 0)$ ,  $Q(1, -2)$  and  $R(0, 2)$  on a rectangular coordinate plane.  
(b) Find the area of  $\triangle PQR$ .

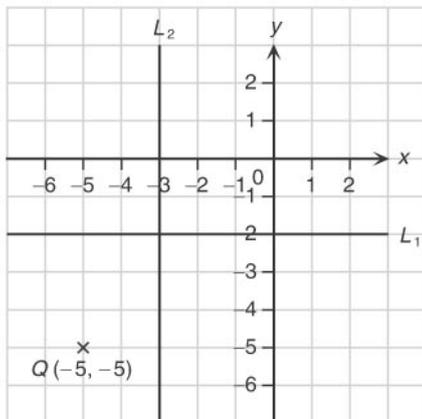
- (a) Draw a parallelogram  $ABCD$  with vertices  $A(-2, 3)$ ,  $B(-5, -1)$ ,  $C(3, -1)$  and  $D(6, 3)$  on a rectangular coordinate plane.
- (b) Find the area of parallelogram  $ABCD$ .

- (a) Draw a pentagon  $ABCDE$  with vertices  $A(-4, 2)$ ,  $B(-2, 4)$ ,  $C(3, 4)$ ,  $D(5, 2)$  and  $E(-1, -2)$  on a rectangular coordinate plane.
- (b) Find the area of pentagon  $ABCDE$ .

$ABCD$  is a parallelogram on a rectangular coordinate plane with vertices  $A(3, -2)$ ,  $B(1, 4)$  and  $C(-4, 4)$ .

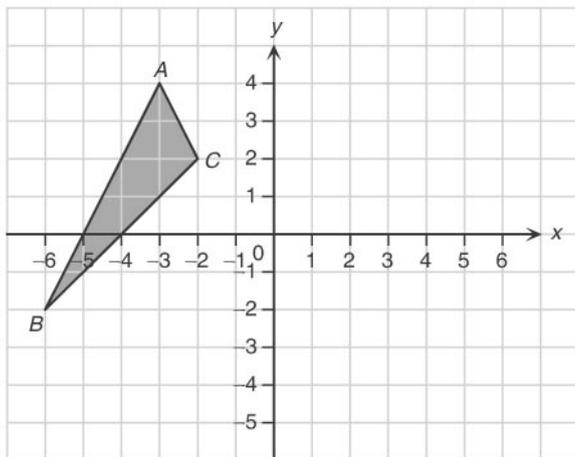
- (a) Find the coordinates of  $D$ .
- (b) Find the area of parallelogram  $ABCD$ .

The figure shows a point  $Q(-5, -5)$ .  $L_1$  is a line parallel to the  $x$ -axis and it passes through  $(0, -2)$ .  $L_2$  is a line parallel to the  $y$ -axis and it passes through  $(-3, 0)$ .



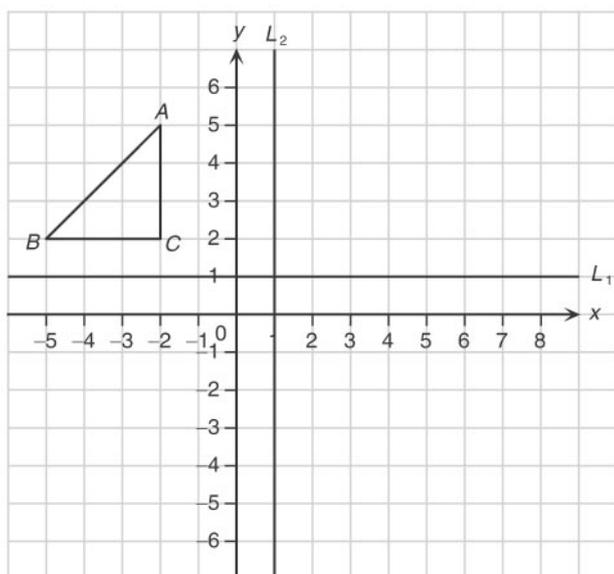
- (a) If  $Q$  is reflected about  $L_1$  to  $Q_1$ , plot  $Q_1$  in the figure and write down its coordinates.
- (b) If  $Q$  is reflected about  $L_2$  to  $Q_2$ , plot  $Q_2$  in the figure and write down its coordinates.

The figure shows  $\triangle ABC$ .



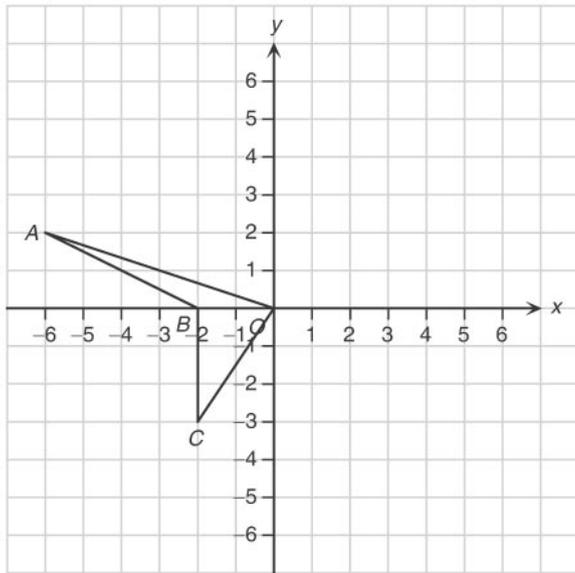
- (a) If  $\triangle ABC$  is translated downwards by 3 units to  $\triangle A_1B_1C_1$ , draw  $\triangle A_1B_1C_1$  in the figure and write down the coordinates of the vertices of  $\triangle A_1B_1C_1$ .
- (b) If  $\triangle A_1B_1C_1$  is reflected about the  $y$ -axis to  $\triangle A_2B_2C_2$ , draw  $\triangle A_2B_2C_2$  in the figure and write down the coordinates of the vertices of  $\triangle A_2B_2C_2$ .

The figure shows  $\triangle ABC$ .



- (a) If  $\triangle ABC$  is reflected about  $L_1$  to  $\triangle A_1B_1C_1$ , draw  $\triangle A_1B_1C_1$  in the figure and write down the coordinates of the vertices of  $\triangle A_1B_1C_1$ .
- (b) If  $\triangle A_1B_1C_1$  is reflected about  $L_2$  to  $\triangle A_2B_2C_2$ , draw  $\triangle A_2B_2C_2$  in the figure and write down the coordinates of the vertices of  $\triangle A_2B_2C_2$ .

The figure shows a quadrilateral  $OABC$ .



- (a) If  $OABC$  is rotated through  $90^\circ$  anti-clockwise about  $O$  to  $O_1A_1B_1C_1$ , draw  $O_1A_1B_1C_1$  in the figure and write down the coordinates of  $O_1$ ,  $A_1$ ,  $B_1$  and  $C_1$ .
- (b) If  $OABC$  is rotated through  $180^\circ$  anti-clockwise about  $O$  to  $O_2A_2B_2C_2$ , draw  $O_2A_2B_2C_2$  in the figure and write down the coordinates of  $O_2$ ,  $A_2$ ,  $B_2$  and  $C_2$ .
- (c) If  $OABC$  is rotated through  $270^\circ$  anti-clockwise about  $O$  to  $O_3A_3B_3C_3$ , draw  $O_3A_3B_3C_3$  in the figure and write down the coordinates of  $O_3$ ,  $A_3$ ,  $B_3$  and  $C_3$ .

Given that  $A(0, 5)$  is rotated through  $90^\circ$  anti-clockwise about the origin  $O$  and then translated upwards by 3 units to  $B$ . Find the area of  $\triangle OAB$ .

Given that  $A(x + 2, 3)$  is the reflection of  $B(-2, y - 1)$  about the  $x$ -axis,

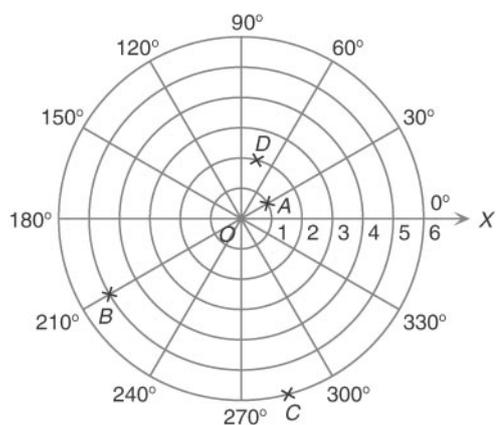
- (a) find  $x$  and  $y$ ,
- (b) write down the coordinates of  $A$  and  $B$ .

Given that  $P(3, 2y + 1)$  is the reflection of  $Q(-x + 2, 5)$  about the  $y$ -axis,

- (a) find  $x$  and  $y$ ,
- (b) write down the coordinates of  $P$  and  $Q$ .

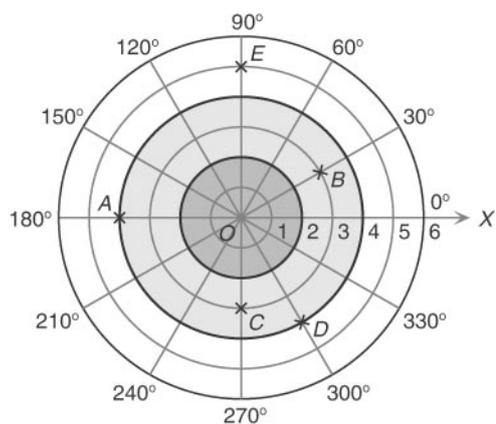
Given that  $M(1, 3y + 1)$  is rotated through  $180^\circ$  anti-clockwise about the origin to  $N(-x + 2, 2)$ ,

- (a) find  $x$  and  $y$ ,
- (b) write down the coordinates of  $M$  and  $N$ .



- (a) Write down the polar coordinates of points  $A$  to  $D$  on the polar coordinate plane.
- (b) Plot  $E(3, 225^\circ)$  and  $F(3, 315^\circ)$  in the figure.
- (c) Plot  $G$  and  $H$  in the figure such that  $EFGH$  forms a square. Write down the polar coordinates of  $G$  and  $H$ .

Helen and Eva are playing an archery game. Each of them shoots five arrows.



- (a) If Helen hits  $A$ ,  $B$ ,  $C$ ,  $D$  and  $E$ , describe the positions of these points by using polar coordinates.
- (b) If Eva hits  $F(1, 15^\circ)$ ,  $G(3, 225^\circ)$ ,  $H(2, 105^\circ)$ ,  $I(2, 300^\circ)$  and  $J(3, 120^\circ)$ , plot these points on the polar coordinates plane.
- (c) If the one whose arrows attain a smaller total distance from  $O$  will be the winner, who will be the winner, Helen or Eva?

- (a) Plot  $A(3, 45^\circ)$ ,  $B(3, 90^\circ)$ ,  $C(3, 135^\circ)$  and  $D(3, 180^\circ)$  on a polar coordinate plane.
- (b) Draw a regular octagon  $ABCDEFGH$  on the polar coordinate plane in (a) and write down the polar coordinates of the other four vertices.

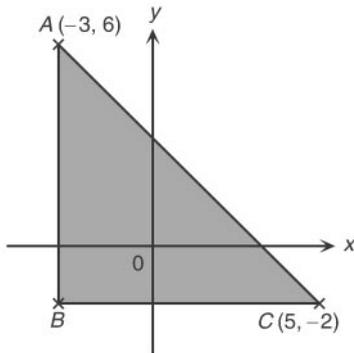
- (a) Plot  $P(4, 60^\circ)$  and  $R(4, 240^\circ)$  on a polar coordinate plane.
- (b) Draw a square  $PQRS$  on the polar coordinate plane in (a) and write down the polar coordinates of the other two vertices.

Plot  $A(2m + 1, m - 5)$  on a rectangular coordinate plane if

- (a)  $A$  lies on the  $x$ -axis,
- (b)  $A$  lies on the  $y$ -axis.

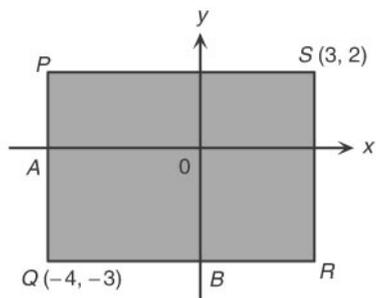
- (a) Plot  $Q(-5, 10)$  on a rectangular coordinate plane and draw a line passing through  $O$  and  $Q$ .
- (b) Determine whether the following points lie on the line drawn in (a).
- (i)  $(2, -1)$
  - (ii)  $(3, -6)$

In the figure,  $A(-3, 6)$  and  $C(5, -2)$  are two vertices of  $\triangle ABC$ .  $AB$  is parallel to the  $y$ -axis and  $BC$  is parallel to the  $x$ -axis.

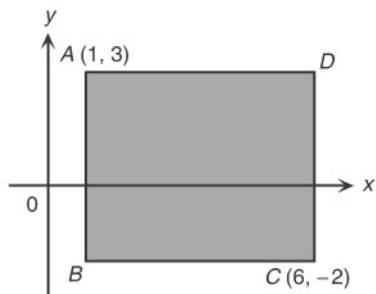


- (a) Write down the coordinates of  $B$ .
- (b) Determine whether the points  $P(-3, 0)$ ,  $Q(-1, -1)$  and  $R(5, 1)$  lie inside, outside or on the side of  $\triangle ABC$ .

In the figure,  $Q(-4, -3)$  and  $S(3, 2)$  are two vertices of rectangle  $PQRS$ .  $PQ$  is parallel to the  $y$ -axis and  $QR$  is parallel to the  $x$ -axis.  $PQ$  cuts the  $x$ -axis at  $A$  and  $QR$  cuts the  $y$ -axis at  $B$ . Find the coordinates of  $P$ ,  $R$ ,  $A$  and  $B$ .

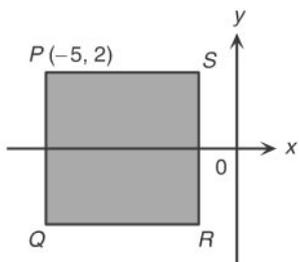


$A(1, 3)$  and  $C(6, -2)$  are two vertices of rectangle  $ABCD$  as shown in the figure.  $AB$  is parallel to the  $y$ -axis and  $BC$  is parallel to the  $x$ -axis.

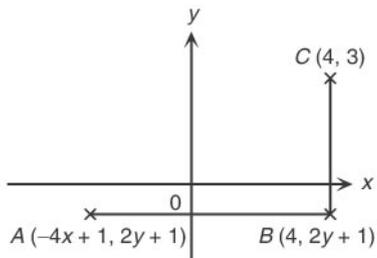


- (a) Find the coordinates of  $B$  and  $D$ .
- (b) Find the perimeter of  $ABCD$ .

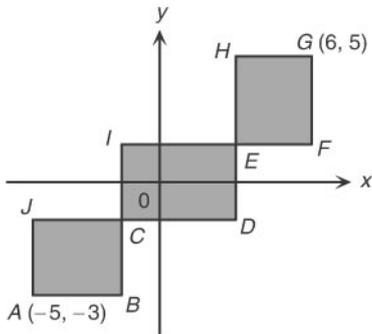
In the figure,  $P(-5, 2)$  is a vertex of square  $PQRS$ . Given that the perimeter of  $PQRS$  is 16 units, find the coordinates of  $Q$ ,  $R$  and  $S$ .



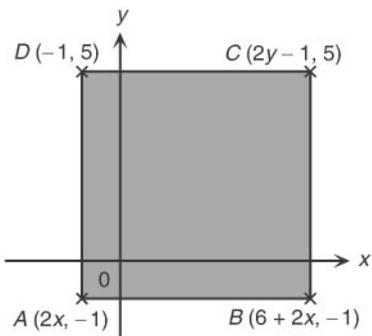
There are three points  $A(-4x + 1, 2y + 1)$ ,  $B(4, 2y + 1)$  and  $C(4, 3)$  in the figure.  $B$  lies on the right of  $A$  and the distance between them is 7 units;  $C$  lies vertically above  $B$  and the distance between them is 4 units. Find  $x$  and  $y$ .



In the figure,  $AB$ ,  $CD$ ,  $EF$ ,  $HG$ ,  $IE$  and  $JC$  are parallel to the  $x$ -axis.  $JA$ ,  $CB$ ,  $ED$ ,  $GF$ ,  $HE$  and  $IC$  are parallel to the  $y$ -axis. If the coordinates of  $A$  and  $G$  are  $(-5, -3)$  and  $(6, 5)$  respectively, find the perimeter of the figure.

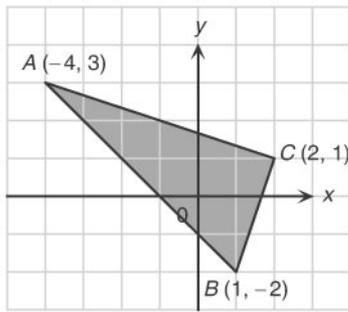


$A(2x, -1)$ ,  $B(6 + 2x, -1)$ ,  $C(2y - 1, 5)$  and  $D(-1, 5)$  formed a square on a rectangular coordinate plane.

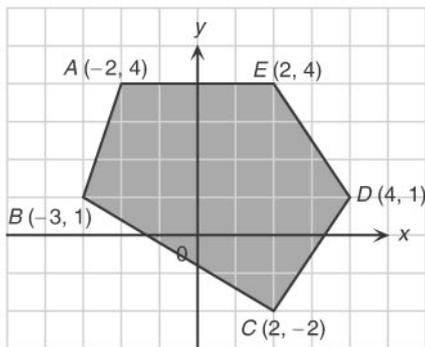


- (a) Find  $AB$ .
- (b) Find  $x$  and  $y$ .

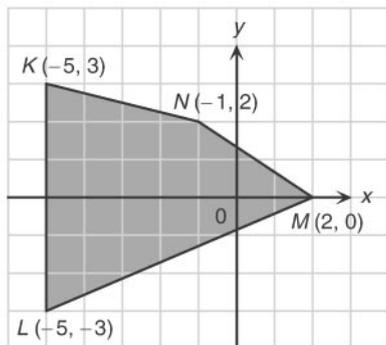
Find the area of  $\triangle ABC$  in the figure.



Find the area of pentagon  $ABCDE$  in the figure.



Find the area of quadrilateral  $KLMN$  in the figure.



## *Ch 10. Introduction to Coordinates*

### **Set 5 Q**

According to the following information, draw rectangle  $ABCD$  on a rectangular coordinate plane.

- (i) The coordinates of  $A$  and  $B$  are  $A(-3, 4)$  and  $B(-3, -1)$  respectively.
- (ii)  $DC$  is on the right of  $AB$ .
- (iii) The length of  $BC$  is two times the length of  $DC$ .

The vertices of rectangle  $ABCD$  are  $A(a - 3, 4)$ ,  $B(-5, b + 1)$ ,  $C\left(\frac{c}{3}, -4\right)$  and  $D\left(6, \frac{2d - 1}{2}\right)$ . It is given that

$AB$  is perpendicular to the  $x$ -axis.

- (a) Find  $a$ ,  $b$ ,  $c$  and  $d$ .
- (b) Write down the coordinates of the vertices of rectangle  $ABCD$ . Which quadrant does each of the vertices lie in?

There are two points  $A\left(-3\frac{1}{2}, -2\right)$  and  $B(5, -2)$  on a rectangular coordinate plane.

- (a) If  $C$  is the reflection of  $B$  about the  $x$ -axis, find the coordinates of  $C$ .
- (b) If  $D$  is the translation of  $A$  upwards by 6 units, find the coordinates of  $D$ .
- (c) Plot points  $A$ ,  $B$ ,  $C$  and  $D$  on a rectangular coordinate plane. What kind of quadrilateral is  $ABCD$ ?
- (d) Find the area of quadrilateral  $ABCD$ .

The vertices of  $\triangle KMN$  are  $K(0, 2)$ ,  $M(-5, -4)$  and  $N(-2, -3)$ . It is given that  $L$  is a line parallel to the  $y$ -axis and it passes through  $(-1, 0)$ .

- (a) Draw  $\triangle KMN$  and line  $L$  on a rectangular coordinate plane.
- (b) If  $\triangle K_1M_1N_1$  is the reflection  $\triangle KMN$  about  $L$ , draw  $\triangle K_1M_1N_1$ .
- (c) Find the area of trapezium  $KK_1MM_1$ .

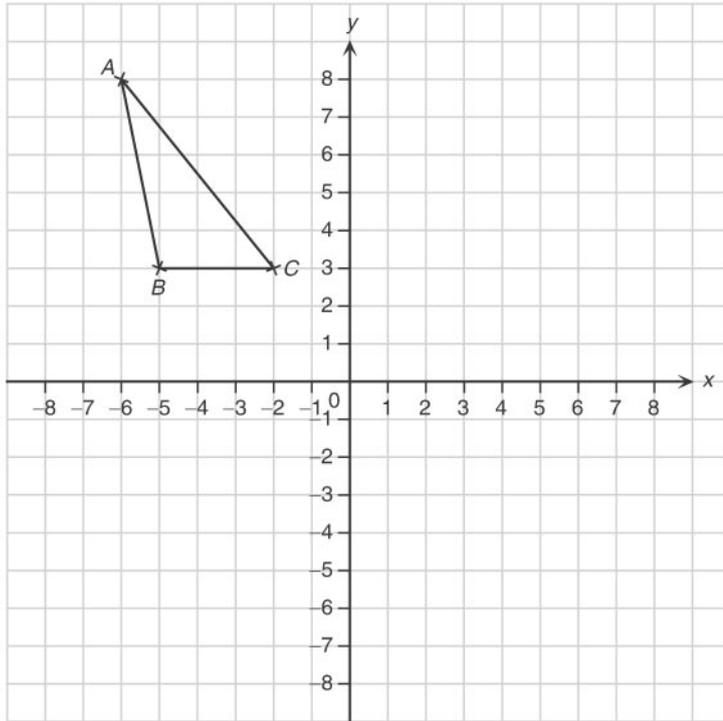
Complete the following table.

	Coordinates before transformation	Type of transformation	Coordinates after transformation
(a)	$A(\_, \_)$	Reflect about the $y$ -axis	$A'(5, -1)$
(b)	$B(\_, \_)$	Translate upwards by 5 units and then translate to the left by 7 units	$B'\left(-4\frac{1}{2}, -8\right)$
(c)	$C(\_, \_)$	Rotate through $90^\circ$ clockwise about the origin and then reflect about the $x$ -axis	$C'(-2, 5)$

Complete the following table.

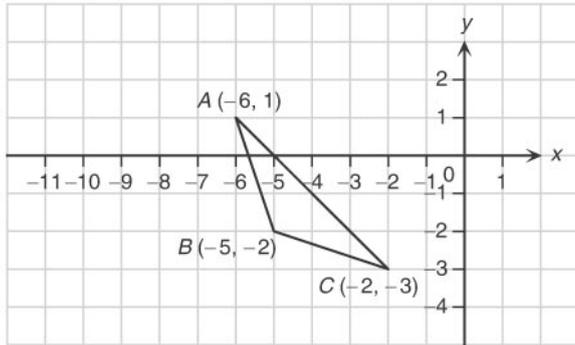
	Coordinates before transformation	Type of transformation	Coordinates after transformation
(a)	$P(\_, \_)$	Reflect about the $y$ -axis and then reflect about the $x$ -axis	$P'(-2, -4)$
(b)	$Q(\_, \_)$	Translate upwards by 4.5 units and then translate to the right by 6.5 units	$Q'(-1, 0)$
(c)	$R(\_, \_)$	Rotate through $270^\circ$ anti-clockwise about the origin and then reflect about the $x$ -axis	$R'(0, -8)$

The figure shows  $\triangle ABC$  with vertices  $A(-6, 8)$ ,  $B(-5, 3)$  and  $C(-2, 3)$ .



- (a) Draw a line  $L$  in the figure such that  $L$  is parallel to the  $y$ -axis and it passes through  $(1, 0)$ .
- (b) If  $\triangle ABC$  is reflected about  $L$  to  $\triangle A_1B_1C_1$ , draw  $\triangle A_1B_1C_1$  in the figure.
- (c) If  $\triangle A_1B_1C_1$  is rotated through  $180^\circ$  anti-clockwise about  $O$  to  $\triangle A_2B_2C_2$ , draw  $\triangle A_2B_2C_2$  in the figure.
- (d) Do  $\triangle ABC$ ,  $\triangle A_1B_1C_1$  and  $\triangle A_2B_2C_2$  have the same shape and size? Find the areas of  $\triangle ABC$ ,  $\triangle A_1B_1C_1$  and  $\triangle A_2B_2C_2$ .

The figure shows  $\triangle ABC$  on a rectangular coordinate plane.

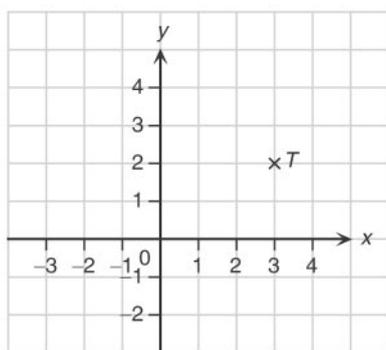


- (a) If  $\triangle ABC$  is reflected about the  $x$ -axis to  $\triangle A_1B_1C_1$ , draw  $\triangle A_1B_1C_1$  in the figure and write down the coordinates of the vertices of  $\triangle A_1B_1C_1$ .
- (b) If  $\triangle ABC$  is rotated through  $270^\circ$  anti-clockwise about  $A$  to  $\triangle AB_2C_2$ , draw  $\triangle AB_2C_2$  in the figure and write down the coordinates of the vertices of  $\triangle AB_2C_2$ .

# Ch 10. Introduction to Coordinates

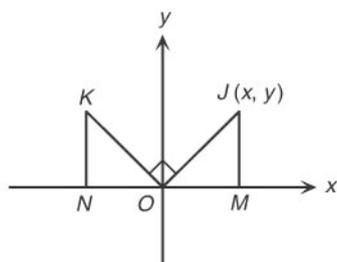
## Set 6 Q

Find the coordinates of  $T$  on the rectangular coordinate plane.



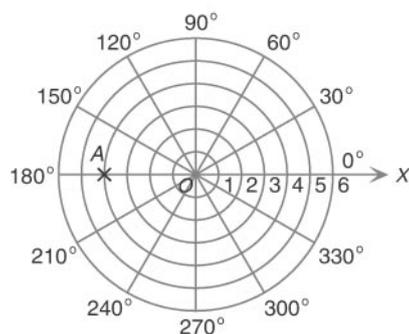
- A. (2, 2)    B. (2, 3)    C. (3, 2)    D. (3, 3)

In the figure,  $K$  is the rotation of  $J(x, y)$  through  $90^\circ$  anti-clockwise about  $O$ . Given that  $KN$  and  $JM$  are both perpendicular to the  $x$ -axis, which of the following is incorrect?



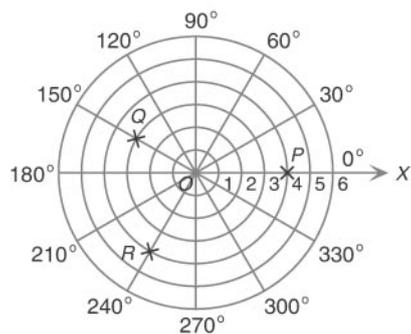
- A.  $OJ = OK$   
 B. The coordinates of  $K$  is  $(-y, x)$ .  
 C. The coordinates of  $M$  is  $(x, 0)$ .  
 D.  $\angle JOM = 45^\circ$

Find the polar coordinates of  $A$  in the figure.



- A.  $(4, 90^\circ)$   
 B.  $(-4, 90^\circ)$   
 C.  $(4, 180^\circ)$   
 D.  $(-4, 180^\circ)$

Find the polar coordinates of  $P$ ,  $Q$  and  $R$  in the figure.

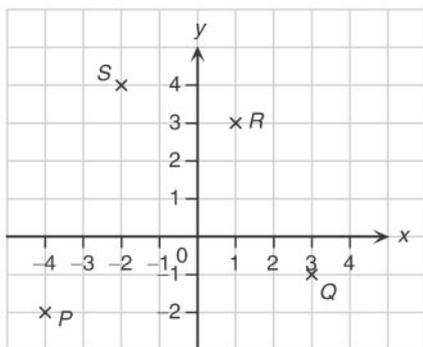


- A.  $P(4, 150^\circ)$ ,  $Q(3, 0^\circ)$ ,  $R(4, 240^\circ)$
- B.  $P(4, 240^\circ)$ ,  $Q(3, 150^\circ)$ ,  $R(4, 0^\circ)$
- C.  $P(4, 150^\circ)$ ,  $Q(3, 240^\circ)$ ,  $R(4, 0^\circ)$
- D.  $P(4, 0^\circ)$ ,  $Q(3, 150^\circ)$ ,  $R(4, 240^\circ)$

On a polar coordinate plane, which of the following two points are not collinear with the pole?

- A.  $(3, 35^\circ)$  and  $(6.5, 215^\circ)$
- B.  $(1, 330^\circ)$  and  $(6, 330^\circ)$
- C.  $(4, 15^\circ)$  and  $(4, 105^\circ)$
- D.  $(7, 124^\circ)$  and  $(7, 304^\circ)$

Which of the following points lies in quadrant II?



- A.  $P$
- B.  $Q$
- C.  $R$
- D.  $S$

$C(-2, 5)$  lies in

- A. quadrant I.
- B. quadrant II.
- C. quadrant III.
- D. quadrant IV.

Given five points  $A(-3, 4)$ ,  $B(4, 4)$ ,  $C(4, 6)$ ,  $D(4, -2)$  and  $E(-3, -2)$ . Which of the following two lines are parallel to the  $x$ -axis?

- A.  $AB$  and  $AC$
- B.  $AB$  and  $DE$
- C.  $AE$  and  $DE$
- D.  $BC$  and  $BD$

The line passing through  $A(-5, 1)$  and  $B(-5, -4)$  is

- A. parallel to the  $x$ -axis.
- B. parallel to the  $y$ -axis.
- C. intersecting with the  $x$ -axis and the  $y$ -axis.
- D. not intersecting with the  $x$ -axis and the  $y$ -axis.

Find the distance between  $A(-3, -2)$  and  $B(-3, -4)$ .

- A. 0 unit
- B. 2 units
- C. 6 units
- D. 8 units

Find the distance between  $A\left(0, -2\frac{5}{11}\right)$  and the origin.

- A. 0 unit
- B.  $-2\frac{5}{11}$  units
- C.  $2\frac{5}{11}$  units
- D.  $\frac{5}{11}$  units

Given a point  $P\left(-5\frac{2}{3}, -2\right)$  and the distance between  $P$  and  $Q$  is  $1\frac{1}{3}$  units, which of the following cannot be the coordinates of  $Q$ ?

- A.  $\left(-6\frac{1}{3}, -2\right)$
- B.  $(-7, -2)$
- C.  $\left(-5\frac{2}{3}, -3\frac{1}{3}\right)$
- D.  $\left(-5\frac{2}{3}, -\frac{2}{3}\right)$

Given two points  $A(-3, 1)$  and  $B(-3, -4)$ , which of the following is/are correct?

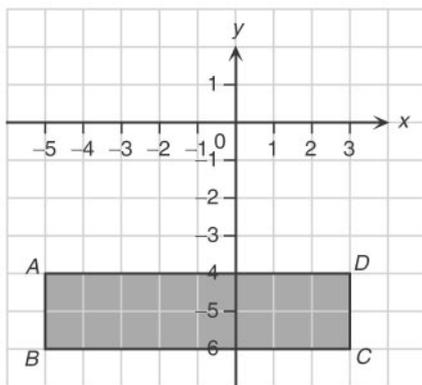
- I.  $AB = 3$  units
  - II.  $AB$  is parallel to the  $y$ -axis.
  - III.  $AB$  intersects with the  $x$ -axis.
- A. I only  
B. III only  
C. II and III only  
D. I and III only

In an equilateral triangle  $ABC$ , the coordinates of the vertices of  $A$  and  $B$  are  $\left(-2, -3\frac{3}{8}\right)$  and

$\left(-2, -1\frac{1}{4}\right)$  respectively. Find the perimeter of  $\triangle ABC$ .

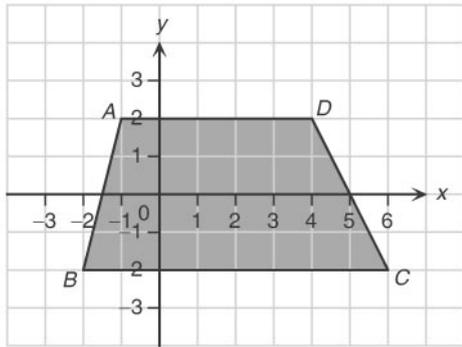
- A.  $2\frac{1}{8}$  units  
B. 4 units  
C.  $4\frac{5}{8}$  units  
D.  $6\frac{3}{8}$  units

Find the area of rectangle  $ABCD$  in the figure.



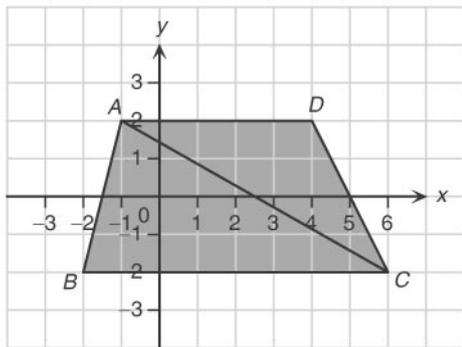
- A. 12 sq. units  
B. 16 sq. units  
C. 18 sq. units  
D. 24 sq. units

Find the area of trapezium  $ABCD$  in the figure.



- A. 13 sq. units
- B. 24 sq. units
- C. 26 sq. units
- D. 29 sq. units

What is the difference between the areas of  $\triangle ABC$  and  $\triangle ACD$ ?



- A. 3 sq. units
- B. 6 sq. units
- C. 8 sq. units
- D. 12 sq. units

On a rectangular coordinate plane, the coordinates of the vertices of  $\triangle PQR$  are  $P(5a, -2)$ ,  $Q(4, -6)$  and  $R(-6, -6)$ . Find the area of  $\triangle PQR$ .

- A. 10 sq. units
- B. 20 sq. units
- C.  $(40a + 48)$  sq. units
- D.  $(40a - 32)$  sq. units

On a rectangular coordinate plane, the coordinates of the vertices of quadrilateral  $EFGH$  are  $E(-1 - 2b, 5)$ ,  $F(1, -4)$ ,  $G(4b, -1)$  and  $H(1, 6)$ , where  $b > 0$ . If the area of  $EFGH$  is 65 sq. units, find  $b$ .

- A. 0.5
- B. 1
- C. 1.5
- D. 2

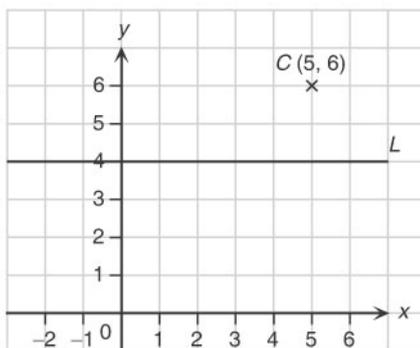
$A(-2, 1)$  is translated to the right by 3 units and then translated upwards by 2 units to  $A_1$ . Find the coordinates of  $A_1$ .

- A. (1, 3)
- B. (1, -1)
- C. (0, 4)
- D. (3, 2)

$R(-3, -2)$  is reflected about the  $x$ -axis to  $R'$ . Find the coordinates of  $R'$ .

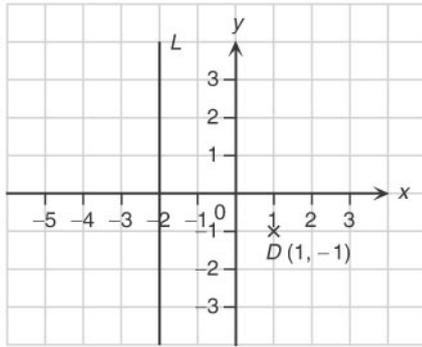
- A. (3, 2)
- B. (3, -2)
- C. (-3, 2)
- D. (-2, 3)

$C(5, 6)$  is reflected about  $L$  to  $C'$ . Find the coordinates of  $C'$ .



- A. (3, 6)
- B. (-5, 6)
- C. (5, 2)
- D. (5, -6)

$D(1, -1)$  is reflected about  $L$  to  $D'$ . Find the coordinates of  $D'$ .



- A.  $(-5, -1)$
- B.  $(-1, -1)$
- C.  $(1, -7)$
- D.  $(5, 1)$

If  $N(5, -8)$  is reflection of  $M(5, -1)$  about line  $L$ , then  $L$  must

- A. pass through  $(5, -4.5)$ .
- B. pass through  $(5, 0)$ .
- C. be perpendicular to the  $x$ -axis.
- D. pass through the origin.

$A(3, -9)$  is rotated through  $180^\circ$  anti-clockwise about the origin to  $A'$ . Find the coordinates of  $A'$ .

- A.  $(-3, -9)$
- B.  $(3, 9)$
- C.  $(9, -3)$
- D.  $(-3, 9)$

$T(-a, b)$  is rotated through  $90^\circ$  anti-clockwise about the origin to  $T'$ . Find the coordinates of  $T'$ .

- A.  $(b, a)$
- B.  $(a, -b)$
- C.  $(-b, a)$
- D.  $(-b, -a)$

$S(-2, 6)$  is translated upwards by 2 units to  $U$ , then  $U$  is rotated through  $90^\circ$  anti-clockwise about the origin to  $W$ . Find the coordinates of  $W$ .

- A.  $(-2, -8)$
- B.  $(-6, 0)$
- C.  $(2, -8)$
- D.  $(-8, -2)$

$A(-2, -3)$  is first reflected about the  $y$ -axis to  $P$ , then  $P$  is rotated through  $90^\circ$  anti-clockwise about the origin to  $Q$ . Find the coordinates of  $P$  and  $Q$ .

- A.  $P(-2, 3), Q(-3, -2)$
- B.  $P(2, -3), Q(3, 2)$
- C.  $P(-3, 2), Q(-3, -2)$
- D.  $P(-3, 2), Q(3, 2)$

Which of the following is true about points  $P(a, b)$  and  $Q(-a, b)$ ?

- A.  $P$  is the reflection of  $Q$  about the  $x$ -axis.
- B.  $Q$  is the reflection of  $P$  about the  $y$ -axis.
- C.  $P$  is the rotation of  $Q$  through  $90^\circ$  anti-clockwise about the origin.
- D.  $Q$  is the rotation of  $P$  through  $180^\circ$  anti-clockwise about the origin.

$P(a, b)$  is rotated through  $180^\circ$  anti-clockwise about the origin  $O$  to  $Q(c, d)$ . Which of the following is/are true?

- I.  $OP = OQ$
  - II.  $a = -c$
  - III.  $b = d$
- A. I only
  - B. II only
  - C. III only
  - D. I and II only