Ch 11. Manipulation of Simple Polynomials

Simplify the following expressions.

- $b^5 \times b^{13}$ **(a)**
- $\frac{25m^{12}}{-5m^4}$ **(b)**
- $(4x^2)(3x^7) \div (6x^3)$ (c)



Determine the degrees of the following polynomials.

- $5x^4 8x^2y^3 + 7xy 4$ **(a)**
- $6x^3y^4 5xy 8x^4$ **(b)**

Simplify the following expressions. (a) $7x + 5x^2 - 2x + x^2$ (b) $5 - 3x^2 + 2x + 6x^2 - 9x + 1$

- 9xyz 4xy + 11xzy 6xz + 12yx(c)

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Write down the constant term and the coefficients of the other terms of the polynomial $8x^3 + 2x^2 - 5$.

For the polynomial $-8a^2 + 5a - 3a^3 - 5$,

- (a) write down the degree of the polynomial,
- (b) arrange the terms in both descending powers and ascending powers of *a* respectively.

Simplify the following expressions.

(a) (4r-s) + (3r-11s)

(b) (-2x-6y+z)-(4x+2y-3z)

Simplify the following expressions and arrange the terms in descending powers of the variables.

- **(a)**
- (6x² 2x + 1) + (-4x² + 2x 5)(5 8y + 7y² y³) (6 4y² + 2y³) **(b)**

Simplify $(6m^3 - 4m^2n + 2mn^2 + 3) - (-2m^3 - 7mn^2 - 9)$.

Simplify $(5a^2 - 6ab - 5) - (3b^2 - 7ab + 10) + (4a^2 + 8b^2 - 2ab)$.

Expand the following expressions by using the distributive law of multiplication.

- (a) 5(x-2y)
- **(b)** (4r - 3s)(-2t)
- (c) $\frac{m}{5}(20-15mn+5m^2)$

Expand the following expressions. (a) (3m+5)(7-2m)

- $(3p-4q)^2$ **(b)**

Find the product of $2a^2 - 3a - 5$ and $4 - 3a^2$, and arrange the terms in descending powers of *a*.

Given the polynomial $4m - 8 + 7m^5 - \frac{1}{2}m^2 - 6m^3$,

- (a) write down the degree and the constant term of the polynomial,
- (b) arrange the terms of the polynomial in descending powers of m,
- (c) find the value of the polynomial when m = 2.

Given $A = x^3 - 5x^2y + 3xy^2 - 4y^3$, $B = 4x^3 + 3x^2y - 5xy^2 - y^3$ and $C = -3x^3 + 4x^2y - 5xy^2 + 3y^3$, (a) find B + (A - C), (b) find B - (A + C).

Expand the following expressions by using the distributive law of multiplication. (a) (7a-4b+9)(-2x)(b) x(3y-2x)-4y(5-x)

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Find the values of the following expressions.

- (a) (+3) (+6)
- **(b)** (-2) (-4)

Find the values of the following expressions. (a) (+9) - (+3) + (-2)

(b) (-10) + (-4) - (-1)

Find the values of the following expressions.

- (a) $(-3) \times (+7)$
- **(b)** $(-5) \times (-6)$

Find the values of the following expressions.

- (a) $\frac{(-6)}{(-9)}$
- **(b)** $(+8) \div (-2)$

Find the values of the following expressions. (a) $(-5) \times (-3) \times (-8)$ (b) $(-3) \times (+2) \div (-4)$

Find the values of the following expressions.

- (a) $(+4) \times (+5) (+7) \times (-3)$
- **(b)** $(-1) \times (+9) + (-16) \div (-2)$

Simplify the following expressions. (a) x + 2x + 3x(b) $-z \times y \times z \times 4$

Simplify the following expressions. (a) $4a \times (-3a)$ (b) $-48b \div 6ab$ Set 2 Q

Simplify the following expressions.

- (a) $b-a \times c + 2b$
- **(b)** $a \times a \times a \times 9 + b \times b \times c \times c^2$

Represent the following word phrases by algebraic expressions.

- (a) Add the product of b and 7c to a.
- (b) Half of the sum of -3x and y.

Represent the following word phrases by algebraic expressions.

- (a) Multiply the square of r by -6.
- (b) Divide q by 5 and then subtract the quotient from p.

By the method of substitution, find the value of the algebraic expression $x^3 - x$ in each of the following cases. (a) x = 2(b) x = -1

By the method of substitution, find the value of the algebraic expression $xy + y^2$ in each of the following cases. (a) x = 1, y = 3

(b) x = -2, y = -1

In each of the following, use the index notation to express the expression.

- (a) $7 \times 7 \times 7$
- **(b)** $2 \times 2 \times 2 \times 2 \times 2$

In each of the following, use the index notation to express the expression. (a) $3 \times 3 \times 7 \times 7 \times 7$

(b) $5 \times 5 \times 2 \times 5 \times 2 \times 2 \times 5$

In each of the following, use the index notation to express the expression.

- (a) $y \times y \times y$
- **(b)** $z \times z \times z \times z \times z \times z$

In each of the following, use the index notation to express the expression.

- (a) $8a \times a \times b \times 8b$
- **(b)** $c \times 3c \times 3c \times c \times 9d$

Find the values of the following expressions without using a calculator.

- **(a)** 3⁴
- **(b)** 2^5

Find the values of the following expressions without using a calculator.

- (a) $2^3 \times 7^2$
- **(b)** $5^2 \times 4^2$

Find the values of the following expressions.

- (a) (-4) + (+6)
- **(b)** (+5) + (-7)

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Find the value of the expression $3^{50} \div 3^{47}$ without using a calculator.

Complete the following operation. -6a - 4b

-) 2*a* + 6*b*

Complete the following operation.

 $x^{2} - 3x + 5$ +) - 2x^{2} - 6

Complete the following operation. $3r^2 + rs$ -) $r^2 + 2rs - 3$

Simplify (3c - 4d) + (5d - 2c).

Simplify $(2b^2 - 7) - (b^2 + 5)$.

Simplify (5a + b - 3) - (3a - 2b + 1).

Simplify (6m - 4 + 2n) - (2m - n + 8).

Simplify $(c^2 + 2c) - (5c - c^2)$.

Simplify (x + 2y) - (3x - 7z) + (6z - 2y).

Expand 5(2m - 3n).

Expand (2a + 3)(-4a).

Expand $3p(2p^2 - p + 5)$.

Expand (n + 7)(n - 3).

Expand (5a - 1)(3 + a) and arrange the terms in descending powers of *a*.

Expand (2x - 3)(3x + 7).

Expand (n-2)(4n-5) by the method of long multiplication.

Expand (2m - 7n)(5m + 3n) by the method of long multiplication.

Expand 3(4d + 1) + 5(3 - 2d).

Expand x(4x + 3) - x(2x - 5).

Expand (3y + 4z)(2z - 7y).

Expand $(3x + 2y)^2$.

Find the value of the expression $\frac{2^{27} \times 5^{18}}{5^{17} \times 2^{25}}$ without using a calculator.

Find the value of the expression $(2^2 \times 2^4) \div (4^{52} \div 4^{49})$ without using a calculator.

Simplify $2m^3 \times m^6$.

Simplify $(0.5k^4)(8k^2)$.

Simplify $-4d^9 \times 3d^2 \times d^3$.

Simplify $\frac{15y^6}{3y^2}$.

Simplify $n^8 \div 5n^5$.

Simplify $54a^8 \div (-9a^3)$.

Simplify
$$\frac{r^8 \times r^5}{4r^4}$$
.

Simplify $\frac{2h^3 \times 3h^9}{24h^6}$.

Simplify $6y^{12} \div y^3 \div (-y^4)$.

Write down the coefficients and the degrees of the following monomials. (a) $17a^3$ (b) $-m^5n^7r^2$

Write down the coefficients and the degrees of the following monomials. (a) $-3ab^2$ (b) $0.12x^4yz^{14}$

Complete the following table.

	Polynomial	Number of	Coe	fficier	nt of	Constant term	Degree of
		terms	x^{3}	x^2	х		polynomial
(a)	$6x^3 - 3x^2 + 2x + 8$						
(b)	$x^3 - \frac{1}{6}x^2 + 9$						

Complete the following table.

	Polynomial	Number of	Coe	fficier	nt of	Constant torm	Degree of
	Folynonnai	terms	x^3	x^2	x	Constant term	polynomial
(a)	$-x^2 + x - 0.6$						
(b)	$\frac{15}{4}x^3 - 2x$						

In each of the following pairs of terms, determine whether they are like terms or unlike terms. (a) $4a^3, 4b^3$

(b) 5, $-\frac{1}{5}$

In each of the following pairs of terms, determine whether they are like terms or unlike terms. (a) $-m^2n$, mn^2

(b) $9xyz, \frac{3xzy}{2}$

Simplify the following expressions. (a) 5x - 4x + 4 - 8(b) 2x - 3y + 3x - 2y

Simplify the following expressions.

- (a) 4m-3-8m+6
- **(b)** 7xy + 2x + 5y 3yx

For the polynomial $7x^2 + 5 - 8x^3 + 6x$,

- (a) write down the degree of the polynomial,
- (b) arrange the terms in both descending powers and ascending powers of x respectively.

For the polynomial $3y^2 - 2 + \frac{y^4}{5} - 6y$,

- (a) write down the degree of the polynomial,
- (b) arrange the terms in both descending powers and ascending powers of y respectively.

Find the value of the polynomial $7 + 5w - 3w^2$ in each of the following cases.

- (a) w = 2
- **(b)** w = -1

Find the value of the polynomial $2y^3 + 4y^2 - y + 1$ in each of the following cases. (a) y = 1

(b) y = -3

Complete the following operation. 3x + 12y<u>+) 2x - 8y</u> Ch 11. Manipulation of Simple Polynomials Set 4 Q

Simplify $\frac{5^{k+2}}{5^k}$.

Simplify $2^{m+7} \times 2^{m-2}$.

Simplify $3w^7 \times 4w^2 \div (-6w^3)$.

Simplify $16c^{15} \div (4c^3 \times 2c^6)$.

Simplify $5k^{12} \div (-2k^8) \div \frac{k^3}{4}$.

Simplify $a^2b^4 \times (-9a^4b^7)$.

Simplify $-64x^5y^6 \div 8x^3y^2$.

Simplify
$$(c^2 \times d^5 \times c^8) \div (d^3 \times c^5 \times d)$$
.

Simplify $4x^7y^3 \div (x^4y^8 \div 2x^3y^5)$.

Simplify
$$32a^5b^8 \div (-2ab^3) \times \frac{5}{8}a^2b$$
.

Write down the degrees and the constant terms of the following polynomials.

(a) $-y + 7x^2y - 13xy^2$ **(b)** $6 + 2a^2bc^3 - 5a^6b^2$

Write down the degrees and the constant terms of the following polynomials.

- (a) $m^3 m^4 n^2 3n + mn^7$ (b) $-5 + x^4 y^5 3z^6 + x^2 y^3 z^6$

Simplify $x^3 - 2x^2 + 7 - 5x^3 + 3x^2 - 6x - 18$.

Simplify $6x^2y - 4xy^2 - 8xy^2 - 11x^2y$.

Simplify $7a^2b - 3b^2a - 2ba^2 + 8ab^2$.

Find the value of the polynomial $2x^2 - \frac{xy}{4} + 1$ in each of the following cases.

(a) x = 2, y = 0(b) x = -1, y = -2

Find the value of the polynomial $3y - x - yx^2$ in each of the following cases.

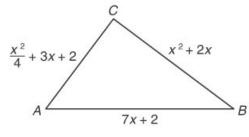
- (a) x = 0, y = -4(b) x = -3, y = 2

There are three jars A, B and C. Jar A contains $(2x^2 + 7)$ candies, jar B contains (21 - 2x) candies and jar C contains $(x^3 - 1)$ candies. If x = 2,

- (a) find the number of candies in each jar,
- (b) determine which jar contains the most number of candies.

In the figure, *ABC* is a triangle. The lengths of its sides are 7x + 2, $x^2 + 2x$ and $\frac{x^2}{4} + 3x + 2$.

- If x = 4,
- (a) find the lengths of AB, BC and CA,
- (b) hence, name the longest side of the triangle *ABC*.



Simplify $(14x^2 - 7 + 5x) - (5 - 6x - 3x^2)$ and arrange the terms in ascending powers of x.

Simplify $3y - [5y - (3y^2 + 12y - 9)]$ and arrange the terms in descending powers of y.

Simplify $(c^3 - 3 + 4c^2) + (9c - 5c^2 - 6) - (11 + 2c^3 - 6c)$ and arrange the terms in descending powers of c.

Simplify $(3gh^2 + 5g^2) - (4h^2 - g^2) + (h^2 - 3gh^2)$.

Simplify $(2b^2a - cb) + (3a^2b + 4bc) - (ab^2 - 2ba^2)$.

(a) Simplify $(m^3 - 4m^2n + 3n^2) + (3m^2n - 2m^3 - 5n^2)$.

(b) Hence, find the value of the expression in (a) when m = -3 and n = 2.

- (a) Simplify $(x^2y + 2x) (-4 + 3xy yx^2) (x^3 3xy + 5)$.
- (b) Hence, find the value of the expression in (a) when x = 2 and y = -5.

A reading club has $(3x^2 + 2x - 1)$ members. $x^2 + 7x$ of them are female members.

- (a) Express the number of male members in terms of x.
- (b) Hence, find the number of male members when x = 3.

Cindy has $(3x^2 - x)$ bookmarks, Janis has $(2 + 4x^2)$ bookmarks and Winnie has $(5x + 2x^2 - 3)$ bookmarks.

- (a) Express the total number of bookmarks they have in terms of x.
- (b) Hence, find the total number of bookmarks when x = 5.

Expand $-4xy(3x^2 - xy - 5y^2)$.

Expand 3(2x + y)(3y - 4x).

Expand $(a^2 + 2)(-3a) - 6a(1 - 2a - a^2)$ and arrange the terms in descending powers of a.

Expand $(1-2x)^2 - (3x+2)(5-2x)$ and arrange the terms in descending powers of x.

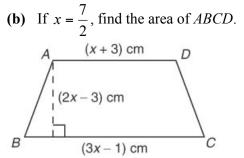
Expand $(p+3q)(p^2-2pq+8q^2)$.

Expand $-2(m-5n)(m^2+3mn+n^2)$.

Janis buys (3x + 4) apples at $\left(\frac{x}{2} - \frac{1}{5}\right)$ each. How much should she pay?

In the figure, *ABCD* is a trapezium. The upper base, lower base and height of *ABCD* are (x + 3) cm, (3x - 1) cm and (2x - 3) cm respectively.

(a) Express the area of ABCD in terms of x.

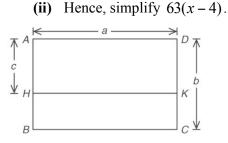


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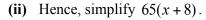
In answering this question, you may need to apply the rules of removing brackets shown below:

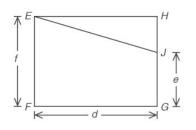
-(r+s) = -r - s

- -(r-s) = -r + s
- (a) (i) In the figure, *ABCD* and *HBCK* are rectangles. By considering the area of rectangle *HBCK*, show that a(b-c) = ab ac.



(b) (i) In the figure, *EFGH* is a rectangle. By using the result of (a)(i) and considering the area of *EFGJ*, show that d(e + f) = de + df.





(c) By using the results of (a)(ii) and (b)(ii), simplify 65(8 + y) - 63(y - 4).

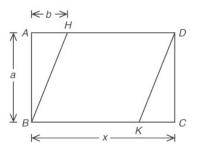
- (a) (i) Given that F = (x+3)(x+1), find the value of F when x = -4. (ii) Hence, if $x^2 + ax + 3 = (x+3)(x+1)$, find the value of a.
- (b) By using the result of (a)(ii), solve $(2x+6)(x+1) 2x^2 = 0$.

In answering this question, you may need to apply the rules of removing brackets shown below:

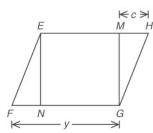
-(r+s) = -r - s

-(r-s) = -r + s

- (a) (i) In the figure, *ABCD* is a rectangle and *HBKD* is a parallelogram. By considering the area of parallelogram *HBKD*, show that a(x b) = ax ab.
 - (ii) Hence, simplify 6(5-2z).



- (b) (i) In the figure, *EFGH* is a parallelogram and *ENGM* is a square. By considering the area of square *ENGM*, show that $(y-c)^2 = y(y-c) c(y-c)$.
 - (ii) By using the results of (a)(i) and (b)(i), simplify $(y-3)^2$.



(c) By using the results of (a)(ii) and (b)(ii), simplify $2(y-3)^2 - 6(5-2y)$.

Consider the following sequence:

7, 13, 25, 49, 97, 193, ...

- (a) Write down the 7th and the 8th terms of the sequence.
- (b) (i) If the first 4 terms are expressed as 7 = 3a + 1, 13 = 3b + 1, 25 = 3c + 1 and 49 = 3d + 1 respectively, find the values of a, b, c and d.
 - (ii) Hence, guess the general term of the sequence.
- (c) Use the result in (b)(ii) to find the 10th and the 12th terms of the sequence.

The table below shows the number of umbrellas (n) sold and the corresponding profit (\$*P*) made by the umbrella shop.

Number of umbrellas sold (<i>n</i>)	200	400	600	800	1000
Profit (\$P)	3800	7800	11 800	15 800	19 800

- (a) Write down a function relating *n* and *P*.
- (b) By using the result of (a), find
 - (i) the value of P when n = 700,
 - (ii) the number of umbrellas sold if the profit is \$8800.
- (c) It is given that the profit is over \$20 000.
 - (i) Set up an inequality to represent the situation.
 - (ii) Find the smallest possible value of *n*.

- (a) Simplify 2(a+b).
- (b) Mary and Candy have 45 marbles altogether, where Mary has *n* marbles. If Mary gives 2 marbles to Candy, the number of Candy's marbles is half of that of Mary's. Without guessing and checking, by using the result of (a), find the value of *n*.

- (a) Simplify $4kx 61 + 48k \div \frac{16}{x} + 28 + 2kx$.
- (b) (i) By using the result of (a), solve 64x + 48x + 32x 33 = 15. (ii) Hence, solve 32y + 24y + 16y - 33 = 15.

Simplify $(4m^2)(-2m^3)$. **A.** $2m^5$ **B.** $2m^6$ **C.** $-8m^5$ **D.** $-8m^6$ Simplify $-27y^{12} \div (-3y^4)$.

A. $9y^3$ **B.** $9y^8$

C. $-9y^3$ **D.** $-9y^8$

Simplify $\frac{(-8a^3)(-a^2)}{2a^4}$. **A.** 4a**B.** $4a^2$ **C.** –4*a* **D.** $-4a^2$

Simplify $3x^{24} \div (6x^2 \times 2x^6)$. **A.** x^2 **B.** x^{28} C. $\frac{1}{4}x^2$ **D.** $\frac{1}{4}x^{16}$

Simplify $4a^4b \times \frac{a^3b^5}{8}$. **A.** $\frac{1}{2}a^7b^6$ **B.** $\frac{1}{2}a^{12}b^5$ C. $\frac{1}{4}a^7b^6$ D. $\frac{1}{4}a^{12}b^5$

Simplify
$$32x^8y^9 \div x^2y^3 \div \left(-\frac{4x^2}{7}\right)$$
.
A. $56x^2y^3$
B. $56x^4y^6$
C. $-56x^2y^3$
D. $-56x^4y^6$

Which of the following is a monomial?

A. $\frac{-m^4}{3}$ **B.** 4m-3 **C.** $\frac{m^3}{n}$ **D.** m-n

- The coefficient of xy^2 in the monomial $-3xy^2$ is
- **A.** −3.
- **B.** −1.
- **C.** 1.
- **D.** 3.

The degree of the monomial $-xy^2z$ is

- **A.** −1.
- **B.** 0.
- C. 2. D. 4.
- **D.** 4

Which of the following is NOT a polynomial?

A.
$$\frac{2}{3}x - 1$$

B. $\frac{x}{y} + 5$
C. -7
D. $\frac{x^2}{4} - \frac{y^2}{3}$

Which of the following is the constant term of the polynomial $3x^3 + 2x^2 - 5x$?

- **A.** -5
- **B.** 0
- **C.** 2
- **D.** 3

The degree of the	polynomial	$2a^2b + 4abc$	$-5a^2b^2c$	is

- **A.** 5.
- **B.** 4.
- **C.** 3.
- **D.** 2.

For the polynomial $1 + 2ab^6 - 7a^4b^2 - 5a^2b^3$, find the number of terms and the coefficient of the term with degree 6.

	Number of terms	The required
		coefficient
А.	3	2
B.	3	-7
С.	4	2
D.	4	-7

Which of the following pairs of terms are like terms?

- **A.** $2a, a^2$
- **B.** $3xy, \frac{1}{2}yx$
- C. $2x^2y, 4y^2x$
- **D.** 5*abc*, 5*ab*

Which of the following is/are correct?

- I. $4x^2 3y^2x + 6$ is a polynomial, but $4x^2$ is not a polynomial.
- **II.** $-3y^2x$ and xy^2 are like terms.
- **III.** 6 is not a monomial.
- A. II only
- B. III only
- C. I and III only
- **D.** I, II and III

Which of the following polynomial is arranged in descending powers of x?

A. $9x - 5x^3 + 2$ B. $3x^4 - 2x^2 + 15$ C. $4 - 2x + 3x^2$

D. $x + 2 + 5x^2$

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If x = -2, the value of the polynomial 4x^2 - 5x + 9 is
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A. 3.

B. 17.

C. 35.

D. 37.

Find the value of the polynomial $\frac{xy}{2} - y^2$ when x = -1 and y = -2. A. 5 B. 3 C. -3 D. -5

Simplify 8x - (3x - 5x). **A.** 0 **B.** 6x**C.** 10x

D. 16*x*

Simplify $3x^2 - 1 + 2x - 6 - 5x^2 + 4x$. **A.** $2x^2 + 6x - 7$ **B.** $2x^2 - 6x - 5$ **C.** $-2x^2 + 6x - 7$ **D.** $-2x^2 - 6x - 5$

Find the constant term in $(4x^2 + 2x + 3) + (3x - 1)$ after simplification.

A. 4

B. 2

C. -2

D. -4

Simplify $(7x^4 + 2 - 3x^2) - (1 - 2x^2 + 2x^3)$ and arrange the terms in ascending powers of x. **A.** $7x^4 - 2x^3 - x^2 + 1$ **B.** $7x^4 - 2x^3 - 5x^2 + 3$

- **C.** $1 x^2 2x^3 + 7x^4$
- **D.** $3-5x^2-2x^3+7x^4$

Simplify
$$(3ba^2 + 2ab^2) - (3b^2a + a^2b)$$
.
A. $4a^2b + ab^2$
B. $3a^2b - 2ab^2$
C. $2a^2b - ab^2$
D. $a^2b + 3ab^2$

Simplify $(3x^3 + 2x^2 + x + 9) + (4 - x^3) + (x^2 - 3x)$. **A.** $2x^3 + 3x^2 - 2x + 13$ **B.** $3x^3 + 3x^2 + x + 13$ **C.** $2x^3 + 3x^2 + x + 4$ **D.** $3x^3 + 3x^2 - 2x + 4$

Find the coefficient of x in the expansion of (3x - 1)(4x + 7). A. 25 B. 21 C. 17

D. 13

Expand $(3x - 4)^2$. A. $9x^2 - 12x - 16$ B. $9x^2 - 12x + 16$ C. $9x^2 - 24x - 16$ D. $9x^2 - 24x + 16$

Expand (2x + y)(3y - x). A. $3y^2 + 2x^2 - 7xy$ B. $3y^2 - 2x^2 + 5xy$ C. $y^3 + 2x^2 - 7xy$ D. $y^3 - 2x^2 + 5xy$ Simplify p(p+q) + q(p-2). **A.** $p^2 + q^2$ **B.** $p^2 + 2pq - 2$ **C.** $p^2 + 2pq - 2q$ **D.** $p^2 + 2pq - q^2$

Expand $(4mn^2 - 3mn + m^4)(-2nm^2)$. **A.** $-8m^3n^3 + 6m^3n^2 - 2m^6n$ **B.** $-8m^2n^4 + 6m^2n^3 - 2m^5n^2$ **C.** $2m^3n^3 - 5m^3n^2 - m^6n$ **D.** $2m^2n^4 - 5m^2n^3 - m^5n^2$

Expand $2(3 - y)(y^2 - 7 + 3y)$. A. $-2y^3 + 4y + 42$ B. $-2y^3 + 32y - 42$ C. $2y^3 + 4y + 42$ D. $2y^3 + 32y - 42$

Subtract $x^2 - 1$ from the product of 2x + 1 and 3x - 2. **A.** $7x^2 - x - 3$ **B.** $7x^2 - 7x - 1$ **C.** $5x^2 - x - 1$ **D.** $5x^2 - 7x - 3$