Chapter 8 Ratio and Rate

## **Multiple Choice**

**1.** If 2x : 3y = 5 : 6, then x : y =A. 2:3 B. 5:4 C. 5:9 D. 12:15

- **2.** If 5: 6 = z: 4, find the value of z.
  - A.  $\frac{11}{3}$  B.  $\frac{10}{3}$  C.  $\frac{8}{3}$  D.  $\frac{7}{3}$
- **3.** Simplify 80¢ : \$4.
  - A. 1:2 B. 2:1 C. 1:5 D. 4:5
- 4. If Chinese workbook has 119 pages and English workbook has 70 pages, find the ratio of the pages of Chinese workbook to that of English workbook.

A. 7:17 B. 10:17 C. 17:7 D. 17:10

5. The figure is formed by identical shapes. Find the ratio of the area of the shaded regions to that of the white regions.



A. 1:2 B. 2:1 C. 2:3 D. 3:2

- **6.** Simplify 2.4 : 0.48.
  - A. 1:2 B. 1:5 C. 2:1 D. 5:1
- 7. Which of the following is equal to  $2\frac{1}{2}:\frac{1}{3}?$ A. 3:10 B. 2:15 C. 15:2 D. 10:3
- 8. If 9: 1 = (8x + 8): 10, find the value of x.
  - A. 9 B. 10 C.  $\frac{39}{4}$  D.  $\frac{41}{4}$

P.1



- 9. Simplify 7 000 cm : 700 m : 0.3 km.
  A. 1 : 10 : 3
  B. 7 : 70 : 30
  C. 700 : 70 : 3
  D. 70 000 : 700 : 3
- **10.** Billy, Peggy and Ben have 2 marbles, 8 marbles and 6 marbles respectively. Find the ratio of the number of marbles each has.

A. 1:3:1 B. 1:4:3 C. 2:3:1 D. 2:3:6

**11.** 84 km/h =

A. 8 400 km/h B. 8 400 m/min C.  $\frac{7}{5}$  m/h D.  $\frac{7}{5}$  km/min

**12.** A certain machine produces 70 plastic bottles in every 130 minutes. Find the speed of production of that machine (in bottles/min).

A.  $\frac{6}{13}$  bottle/min B.  $\frac{7}{13}$  bottle/min C.  $1\frac{1}{7}$  bottles/min D.  $1\frac{6}{7}$  bottles/min

- **13.** Given a:b:c=1:2:3. If a=9, find b+c.A. 18B. 27C. 45D. 54
- 14. The sum of all interior angles of a pentagon is  $540^{\circ}$ . If the ratio of the 5 interior angles of the pentagon is 2:3:4:3:3, find the smallest angle.

A. 72° B. 101.25° C. 108° D. 202.5°

- **15.** In a box of eggs, the ratio of the number of rotten eggs to that of broken eggs are 1 : 7, and the ratio of the number of broken eggs to that of good eggs are 2 : 5. If there are totally 10 rotten eggs, find the total number of eggs in the box.
  - A. 60 B. 70 C. 175 D. 255
- **16.** The price of Brand A, B and C green tea are \$5.2, \$6.5 and \$7.8 respectively. Find the ratio of the prices of Brand A, B and C green tea.

A. 3:4:5 B. 4:5:6 C. 5:6:7 D. 6:7:8

17. The total marks of Mathematics examination is 90. It is known that the full marks of parts A, B and C are in the ratio of 3 : 2: 4. Find the full mark of part A.

A. 60 B. 40 C. 30 D. 20

18. The different plans of mobile phone of Apple Telephone Company are as follows:

|          | Monthly fee | Airtime (min) |
|----------|-------------|---------------|
| Plan A:  | \$65        | 100 min       |
| Plan B : | \$153       | 180 min       |
| Plan C : | \$256       | 320 min       |
| Plan D:  | \$369       | 450 min       |

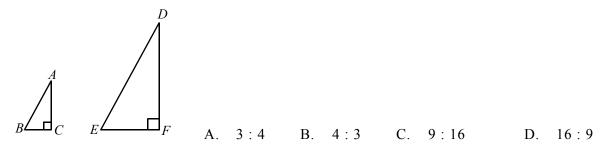
According to the monthly fee and airtime of different plans, which is the cheapest for each minute?

A. Plan A B. Plan B C. Plan C D. Plan D

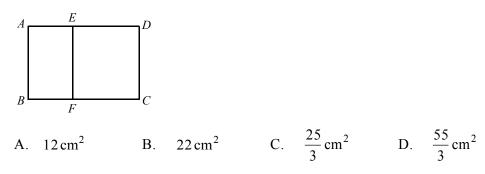
19. Jacky typed 20 Chinese words in  $1\frac{1}{4}$  minutes, Mandy typed 8 Chinese words in 40 seconds. Find the ratio of the typing speed of Jacky to that of Mandy.

A. 1:5 B. 4:3 C. 4:15 D. 4:75

- **20.** Karen drives at a speed of 52 km/h for 1.5 hours, then at a speed of 50 km/h for 0.7 hour. How far has she travelled?
  - A. 102 km B.  $106 \frac{2}{21} \text{ km}$  C. 111.4 km D. 113 km
- **21.** In the figure, each side of  $\triangle ABC$  is multiplied by  $\frac{4}{3}$  to form  $\triangle DEF$ . Find the ratio of the area of  $\triangle ABC$  to that of  $\triangle DEF$ .



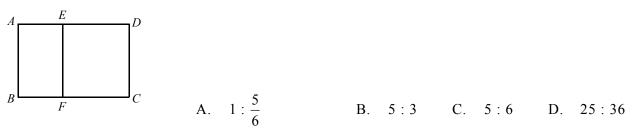
**22.** The figure shows rectangle *ABFE* and rectangle *CDEF*. If BF : FC = 5 : 6 and the area of rectangle *ABFE* is  $10 \text{ cm}^2$ , find the area of rectangle *CDEF*.



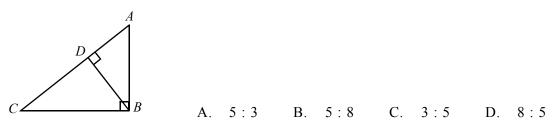
Email: mathspercyyeung@gmail.com

created by Percy Yeung

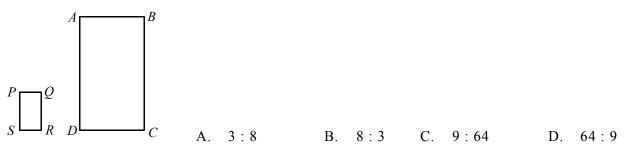
**23.** In the figure, *ABFE* is a rectangle, *CDEF* is a square. If the area of rectangle *ABFE* and that of square *CDEF* are in the ratio of 5 : 6, find *AE* : *ED*.



**24.** In the figure,  $\triangle ABD$  and  $\triangle ACB$  are right-angled triangles. *D* is a point on *AC*. If the area of  $\triangle ABD$  and that of  $\triangle ACB$  are in the ratio of 5 : 8, find *AD* : *AC*.



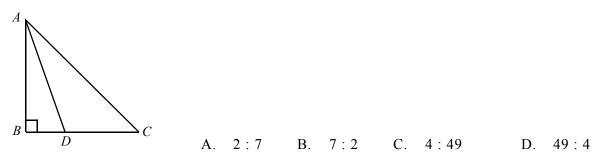
25. In the figure, both the length and width of rectangle *ABCD* are  $\frac{8}{3}$  times those of rectangle *PQRS*. Find the ratio of the area of rectangle *ABCD* to that of rectangle *PQRS*.



26. It is known that the speed of sound is 340 m/s. If David shouts at a perpendicular slope and he can hear his echo in 8 seconds, find the distance between David and the slope.

| A. | 2 720 m | Β. | 1 360 m | C. | 340 m | D. | 42.5 m |
|----|---------|----|---------|----|-------|----|--------|
|----|---------|----|---------|----|-------|----|--------|

**27.** The figure shows  $\triangle ABC$ . *D* is a point on *BC* such that BD : DC = 2 : 7. If *AB* is the height of  $\triangle ABC$ , find the ratio of the area of  $\triangle ABD$  to that of  $\triangle ADC$ .

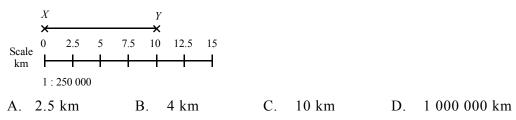


created by Percy Yeung

**28.** Express the scale 3 cm to 21 km in the form of 1 : n.

A. 1:7 B. 1:7000 C. 1:100000 D. 1:700000

**29.** Find the actual length of the line *XY*.



**30.** The scale of a map is 1 : 100. If the actual distance is 7 km, find the distance on the map.

A. 7 m B. 70 m C. 700 m D. 7 km

**31.** The scale of a map is 1 : 250 000, and the length of the subway on the map is 0.6 cm. If a car travelled through the subway at a constant speed in 2 minutes. Find the speed of that car in km/h.

A. 45 km/h B. 90 km/h C. 95 km/h D. 135 km/h

**32.** The scale of a map is 2 : 6 000. If the actual area of a reservoir is 10 000 m<sup>2</sup>, find the area of that reservoir on the map.

A.  $1\frac{2}{3}$  cm<sup>2</sup> B.  $3\frac{3}{10}$  cm<sup>2</sup> C.  $11\frac{1}{9}$  cm<sup>2</sup> D. 9 000 000 cm<sup>2</sup>

**33.** The scale of a map is 1 : 200. If the actual area is 3 600 000 cm<sup>2</sup>, find the corresponding area on the map.

A.  $90 \text{ cm}^2$  B.  $1\ 800 \text{ cm}^2$  C.  $18\ 000 \text{ cm}^2$  D.  $720\ 000\ 000\ \text{cm}^2$ 

**34.** The scale of a map is 1 cm to 1 m. If the area of a square flower-bed on the map is 11 cm<sup>2</sup>, find the actual area of that flower-bed.

A.  $11 \text{ m}^2$  B.  $1 100 \text{ m}^2$  C.  $110 000 \text{ m}^2$  D.  $11 000 000 \text{ cm}^2$ 

**35.** The scale of a map is 1 : 200 000. If the actual length of a highway is 26 km, find the length of that highway on the map.

A. 2 cm B. 13 cm C. 26 cm D. 52 cm

## Section A(1)

- 1. Simplify the following ratios.
  - (a) 16:20 (b) 0.91:0.26 (c)  $\frac{3}{2}:\frac{12}{7}$
- 2. Simplify the following ratios.

(a) 2 weeks : 4 days (b) 10 km : 25 cm (c)  $180^{\circ}$  :  $\frac{3}{5}$  right-angle

- **3. (a)** If  $\frac{3}{5} = \frac{x}{45}$ , find the value of x.
  - (b) If 5: 4 = y: 24, find the value of y.
  - (c) If 2: 5 = 10: z, find the value of z.
- **4.** Each of the following figures is formed by identical shapes. Find the ratio of the area of the shaded regions to that of the white regions.



- 5. John's weight is 52 kg. His father's weight is 78 kg. Find the ratio of John's weight to his father's.
- 6. The costs of two computers are in the ratio of 4 : 6. If the cost of the cheaper one is \$8 400, find the cost of the more expensive one.
- 7. If a : b = 2 : 5 and b : c = 3 : 7, find a : b : c.
- 8. If  $\frac{1}{a}:\frac{1}{b}:\frac{1}{c}=3:4:9$ , find a:b:c.

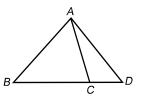
- 10. Express the rates of the following in the units stated in the brackets.
  - (a) The price of 4 kg of beef is 48. (kg)
  - (b) The rent of a flat is \$8 100 for  $2\frac{1}{2}$  months. (\$/month)

11. A motor car runs 810 km in 9 hours and a train runs 567 km in 6 hours. Which vehicle runs faster?

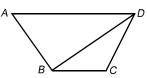
- 12. A car took 35 minutes to travel 70 km, find the speed of the car(a) in km/h.(b) in m/s.
- 13. John completed 7 rounds in a 400 m field in 14 minutes, find his speed in km/h.
- 14. Express the scale below in the form of 1 : n.

(a) 20 mm : 4 000 cm (b) 0.65 cm : 13 m (c) 2.5 cm : 1 km

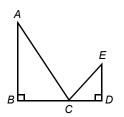
- 15. On a map, an actual distance of 12 km is represented by 0.6 cm. What is the scale of the map?
- **16.** The scale of a map is 1 : 80 000. If the actual distance between two buildings is 640 m, find their distance on a map (in cm).
- 17. In the figure, *BCD* is a straight line and *BC* : CD = 2 : 1. Find the ratio of the area of  $\triangle ABC$  to that of  $\triangle ACD$ .



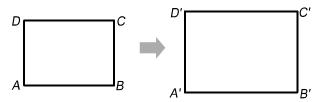
**18.** The figure shows trapezium *ABCD*. If the ratio of the area of  $\triangle BCD$  to that of  $\triangle ABD$  is 4 : 7, find *BC* : *AD*.



**19.** In the figure, *ABC* and *CDE* are two right-angled triangles where *AB* : *DE* = 5 : 3 and *BC* : *CD* = 5 : 2. Find the ratio of the area of  $\triangle ABC$  to that of  $\triangle CDE$ .



**20.** In the figure, rectangle A'B'C'D' is obtained when each side of rectangle *ABCD* is enlarged by 0.25. Find the ratio of the area of rectangle *ABCD* to that of rectangle *A'B'C'D'*.



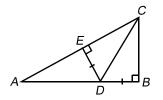
## Section A(2)

- **21.** Simplify the following ratios.
  - (a)  $1.75: 1\frac{2}{3}$  (b)  $50 \text{ cm}^3: 0.1 \text{ L}$  (c) 30 minutes: 0.5 hour
- 22. A and B share \$3 600 in the ratio of 1 : 8. How much does each of them receive?
- **23.** If the cost of 5 apples is \$12.5, and the cost of 8 oranges is \$24, find the ratio of the cost of each apple to that of orange.
- 24. There are 1 200 students in the Diligent Secondary School. Among them, 500 are boys.Find the ratio of
  - (a) the number of boys to the total number of students.
  - (b) the number of girls to the total number of students.
  - (c) the number of boys to the number of girls.
- 25. A sum of \$1 200 is divided among Mary and Tom. Mary gets 3 times as many as Tom.
  - (a) Find the ratio of the amount Mary gets to that of Tom.
  - (b) How much does Mary get?

Email: mathsperçyyeung@gmail.com

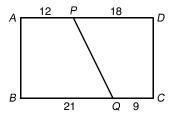
- **26.** If x : y : z = 2 : 3 : 4 and x + y + z = 27, find the values of x, y and z.
- **27.** A sum of \$3 900 is divided among Jacky, Jenny and Susan. The ratio of the amount Jacky gets to that of Jenny is 2 : 3, the ratio of the amount Jenny gets to that of Susan is 2 : 1. How much does each one get?
- **28.** Given that a : b : c = 9 : 8 : 5.
  - (a) Prove  $\frac{1}{a}:\frac{1}{b}=8:9.$  (b) Find  $\frac{1}{b}:\frac{1}{c}$ . (c) Find  $\frac{1}{a}:\frac{1}{b}:\frac{1}{c}$ .
- **29.** The ratio of basketballs, volleyballs and footballs in a bag is 2 : 3 : 5. If there are 9 volleyballs in the bag,
  - (a) find the total number of balls.
  - (b) find the number of footballs in the bag.
- **30.** A car used 50 litres of petrol to travel 450 km.
  - (a) How far does it travel for each litre of petrol on average?
  - (b) To travel 1 km, how much petrol is required?
  - (c) For a journey of 432 km, how much petrol is required?
- **31.** Suppose that 4 US dollars can be exchanged with HK\$30 and 16 Japanese Yen can be exchanged with HK\$1.
  - (a) How many HK dollars can be exchanged with 50 US dollars?
  - (b) How many Japanese Yen can be exchanged with 50 US dollars?
  - (c) How many Japanese Yen can be exchanged with 1 US dollars?
- 32. On a map of scale 1 : 25 000, the length of a certain road is 4.5 cm. Find
  - (a) the actual length of the road in km.
  - (b) the length of the road, in cm, on another map with the scale of 1 : 75 000.

**33.** In the figure, DE = DB and  $\angle CED = \angle CBD = 90^{\circ}$ . If AC : BC = 13 : 5, find the ratio of the area of  $\triangle ACD$  to that of  $\triangle BCD$ .



## Section **B**

- 34. Suppose the cost of painting a wall is in proportion to the area of the wall. Given the cost of painting a 28 m (length) by 2.5 m (height) wall is \$5 000. There is another wall of which the length is 50% longer and the height is 10% shorter than the wall mentioned above.
  - (a) Find the ratio of the area of the new wall to that of the given one.
  - (b) Find the cost of painting the new wall.
- **35.** In the figure, *ABCD* is a rectangle with AP = 12, PD = 18, BQ = 21 and QC = 9.



- (a) Find the ratio of the area of trapezium ABQP to that of trapezium PQCD.
- (b) If the area of the trapezium ABQP is 297 square units, find the area of the trapezium PQCD.